

# Parity Violation: Past, Present, and Future



M.J. Ramsey-Musolf



# NSAC Long Range Plan

- What is the structure of the nucleon?
- What is the structure of nucleonic matter?
- What are the properties of hot nuclear matter?
- What is the nuclear microphysics of the universe?
- What is to be the new Standard Model?

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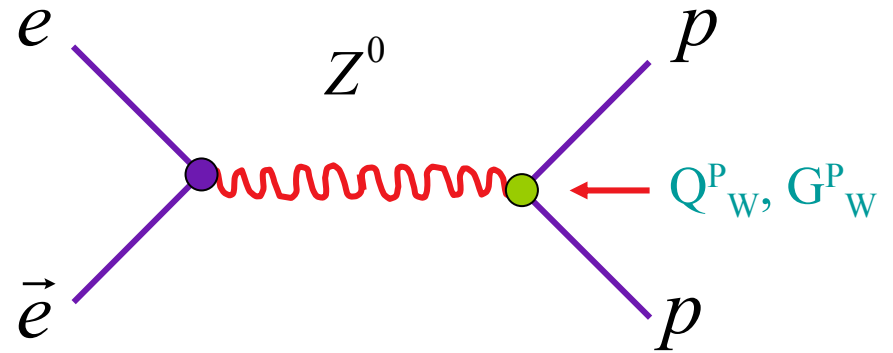
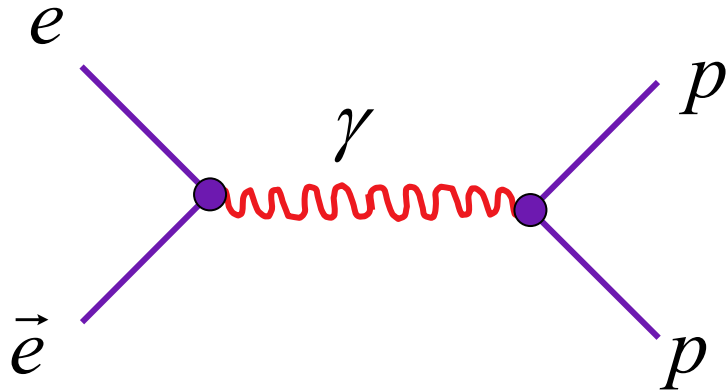


**Parity-Violating Electron Scattering**

# Outline

- PVES and Nucleon Structure
- PVES and Nucleonic Matter
- PVES and the New Standard Model

# Parity-Violating Asymmetry

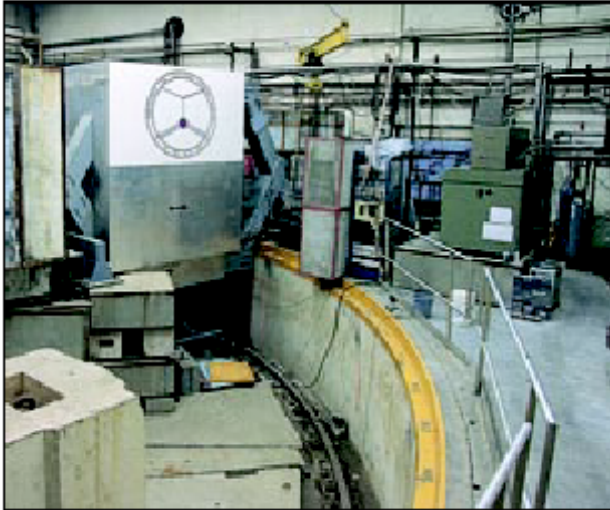


$$A_{LR} = \frac{N_+ - N_-}{N_+ + N_-} = \frac{2 \operatorname{Re} A_{PV} A_{PC}^*}{|A_{PC}|^2}$$

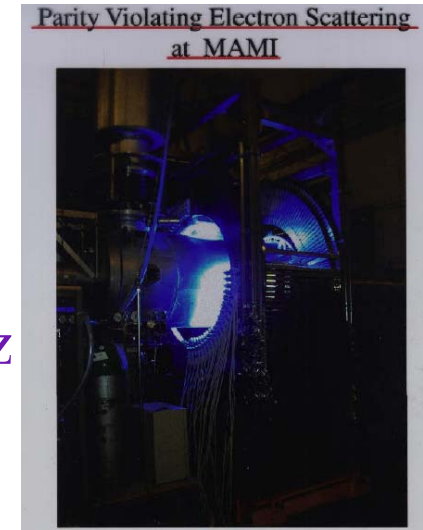
$$= \frac{G_F |Q^2|}{4\sqrt{2}\pi\alpha} \left[ Q_W^P + F(Q^2, \theta) \right]$$

A red arrow points from the term  $G_W^P$  in the second equation to the  $G_W^P$  term in the first equation.

# PV Electron Scattering Experiments



MIT-Bates



Mainz

Jefferson  
Lab



SLAC

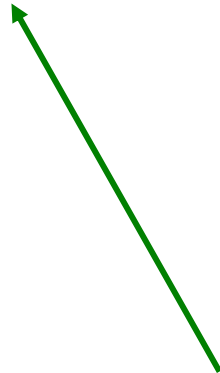


# PV Electron Scattering Experiments

Deep Inelastic eD (1970's)

PV Moller Scattering (now)

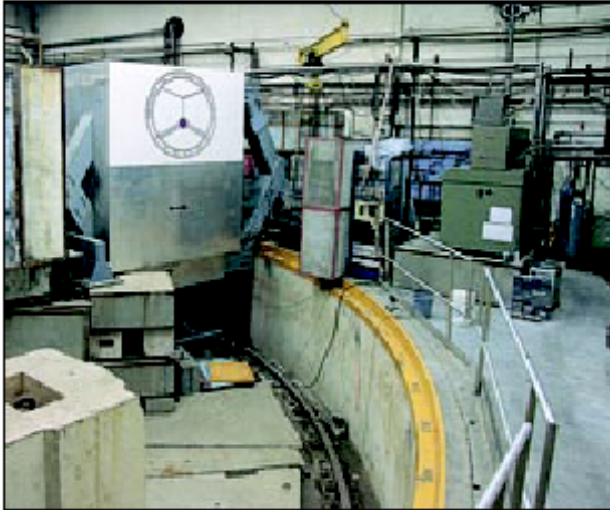
Deep Inelastic eD (2005?)



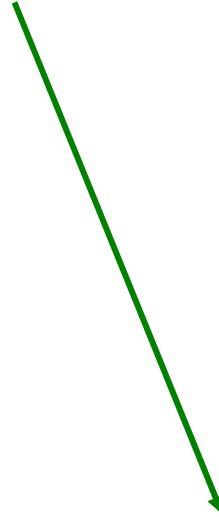
SLAC



# PV Electron Scattering Experiments



MIT-Bates

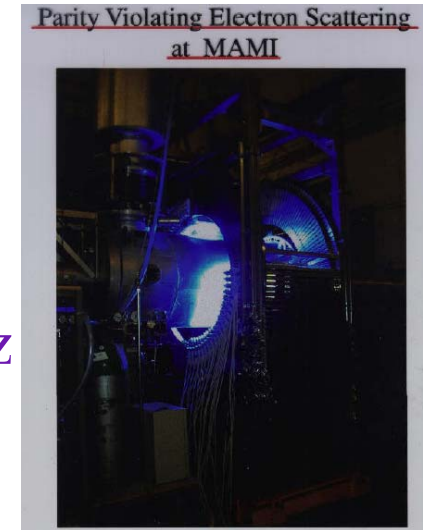


Elastic  $e\ ^{12}\text{C}$  (1970's - 1990)

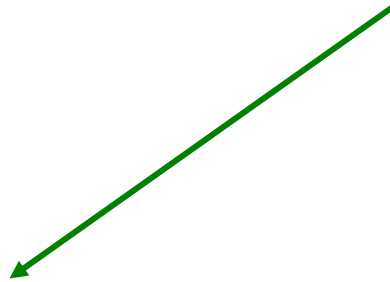
Elastic  $ep$ , QE  $eD$  (1990's - now)



# PV Electron Scattering Experiments



Mainz



QE  $e$   $^9\text{Be}$  (1980's)

Elastic  $ep$  (1990's - now)

# PV Electron Scattering Experiments

Elastic ep: HAPPEX, G0 (1990's - now)

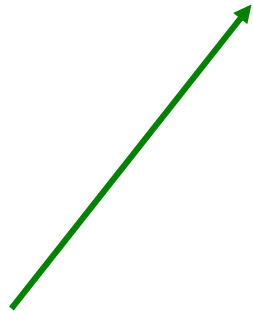
Elastic e  $^4\text{He}$ : HAPPEX (2003)

Elastic e  $^{208}\text{Pb}$ : PREX

QE eD, inelastic ep: G0 (2003-2005?)

Elastic ep: Q-Weak (2006-2008)

Moller, DIS eD (post-upgrade?)

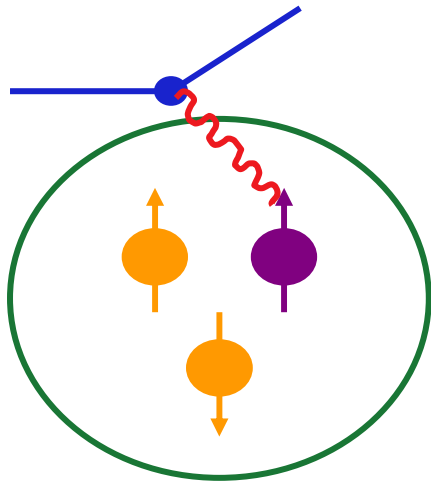


Jefferson  
Lab



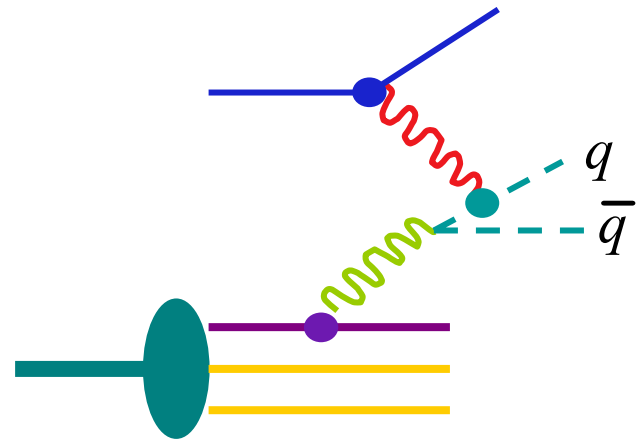
# PVES and Nucleon Structure

What are the relevant degrees of freedom for describing the properties of hadrons and why?



Constituent quarks (QM)

$$Q^P, \mu^P$$



Current quarks (QCD)

$$F_2^P(x)$$

# PVES and Nucleon Structure

Why does the constituent Quark Model work so well?

- Sea quarks and gluons are “inert” at low energies
- Sea quark and gluon effects are hidden in parameters and effective degrees of freedom of QM (Isgur)
- Sea quark and gluon effects are hidden by a “conspiracy” of cancellations (Isgur, Jaffe, R-M)
- Sea quark and gluon effects depend on C properties of operator ( $J_i$ )

# PVES and Nucleon Structure

What are the relevant degrees of freedom for describing the properties of hadrons and why?

Strange quarks in the nucleon:

- Sea quarks
- $m_s \sim \Lambda_{\text{QCD}}$
- 20% of nucleon mass, possibly -10% of spin

What role in electromagnetic structure ?

# We can uncover the sea with $G^P_W$

Light QCD quarks:

$$u \quad m_u \sim 5 \text{ MeV}$$

$$d \quad m_d \sim 10 \text{ MeV}$$

$$s \quad m_s \sim 150 \text{ MeV}$$

Heavy QCD quarks:

$$c \quad m_c \sim 1500 \text{ MeV}$$

$$b \quad m_b \sim 4500 \text{ MeV}$$

$$t \quad m_t \sim 175,000 \text{ MeV}$$

Effects in  $G^P$  suppressed by

$$(\Lambda_{\text{QCD}}/m_q)^4 < 10^{-4}$$

$$\Lambda_{\text{QCD}} \sim 150 \text{ MeV}$$



Neglect  
them

# We can uncover the sea with $G_W^P$

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$m_s \sim \Lambda_{\text{QCD}}$  : No suppression

not necessarily negligible

# We can uncover the sea with $G_W^P$

Light QCD quarks:

u  $m_u \sim 5 \text{ MeV}$

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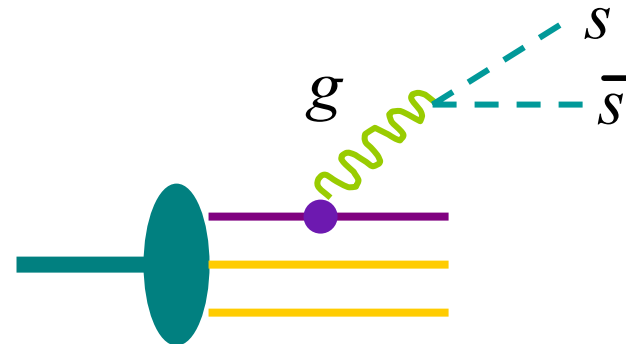
Heavy QCD quarks:

c  $m_c \sim 1500 \text{ MeV}$

b  $m_b \sim 4500 \text{ MeV}$

t  $m_t \sim 175,000 \text{ MeV}$

Lives only in the sea





# Parity-Violating Electron Scattering

Kaplan and Manohar  
McKeown

## Neutral Weak Form Factors

$$G^P = Q^u G^u + Q^d G^d + Q^s G^s \longleftrightarrow \gamma$$

$$G^n = Q^u G^d + Q^d G^u + Q^s G^s \longleftrightarrow \gamma, \text{ isospin}$$

$$G_W^P = Q_W^u G^u + Q_W^d G^d + Q_W^s G^s \longleftrightarrow Z^0$$

 SAMPLE (MIT-Bates), HAPPEX  
(JLab), PVA4 (Mainz), G0 (JLab)

  $G^u, G^d, G^s$

  
 $G^u, G^d, G^s$

# Parity-Violating Electron Scattering

Separating  $G_W^E, G_W^M, G_W^A$

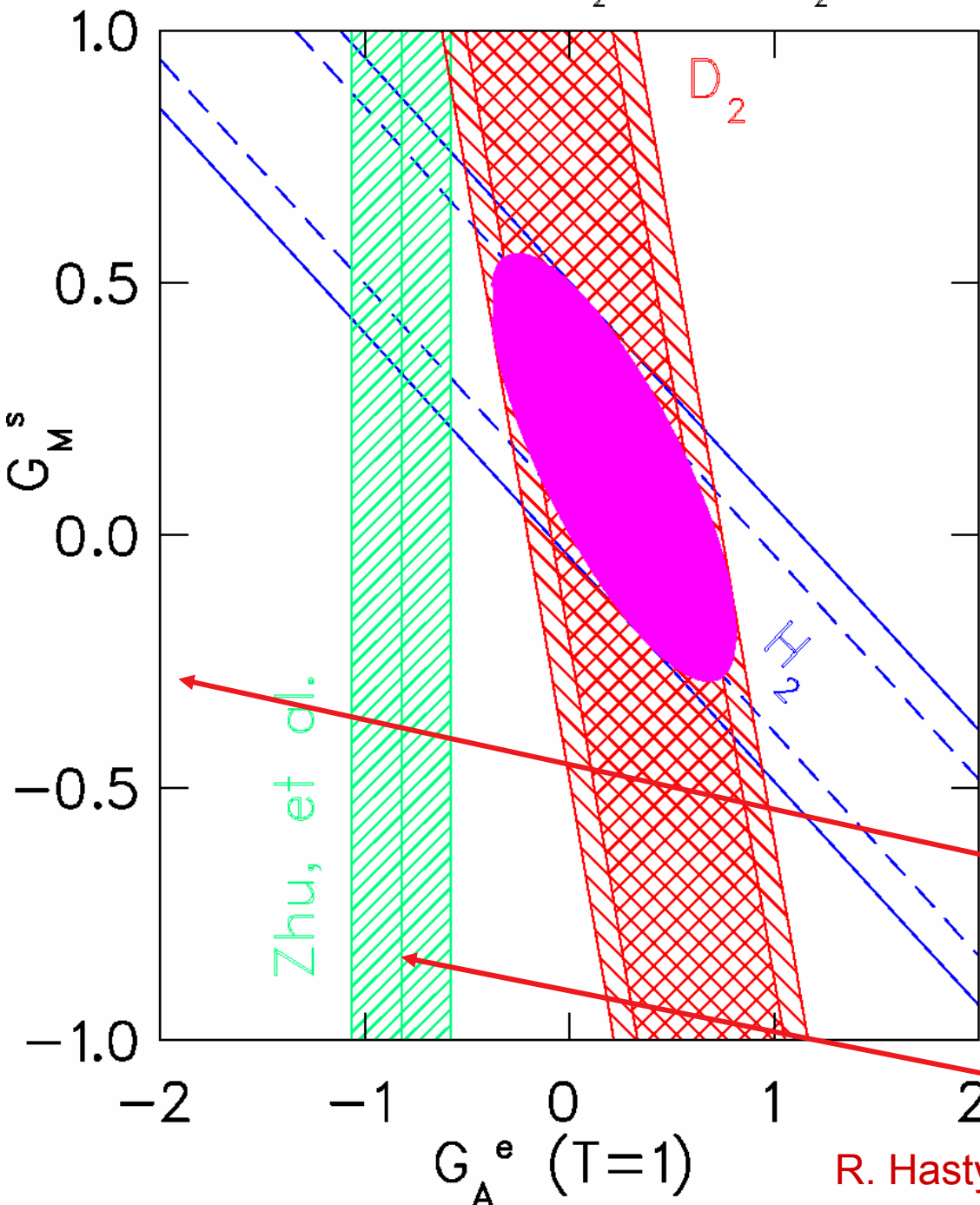
$G_W^M, G_W^A$  SAMPLE

$G_W^M, G_W^E$  HAPPEX, PVA4

$G_W^M, G_W^E, G_W^A$  :  $Q^2$ -dependence G0

Published results: SAMPLE, HAPPEX

SAMPLE Combined 98 H<sub>2</sub> and 99 D<sub>2</sub> data



at  $Q^2=0.1$  (GeV/c)<sup>2</sup>

$$G_M^s = 0.14 \pm 0.29 \pm 0.31$$

$$G_A^e(T=1) = 0.22 \pm 0.45 \pm 0.39$$

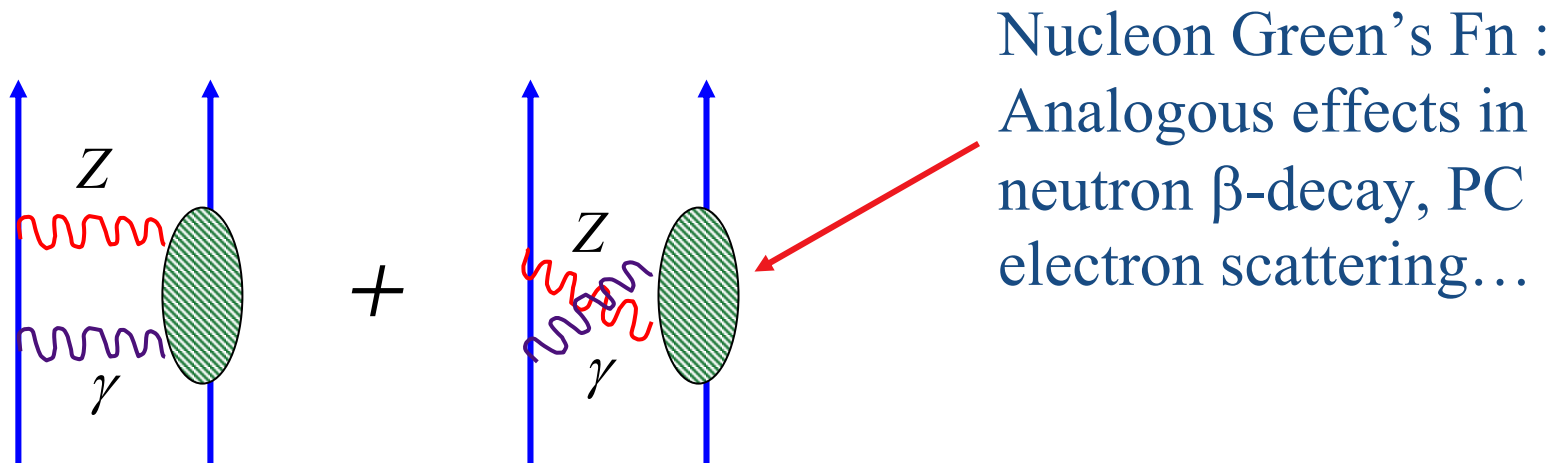
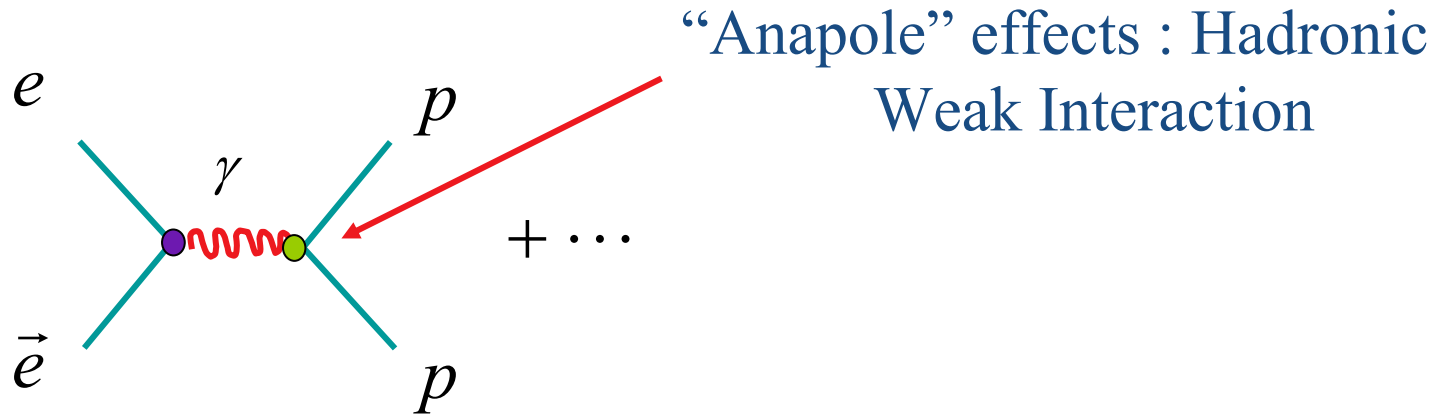
- s-quarks contribute less than 5% ( $1\sigma$ ) to the proton's magnetic form factor.
- proton's axial structure is complicated!

Models for  $\mu^s$

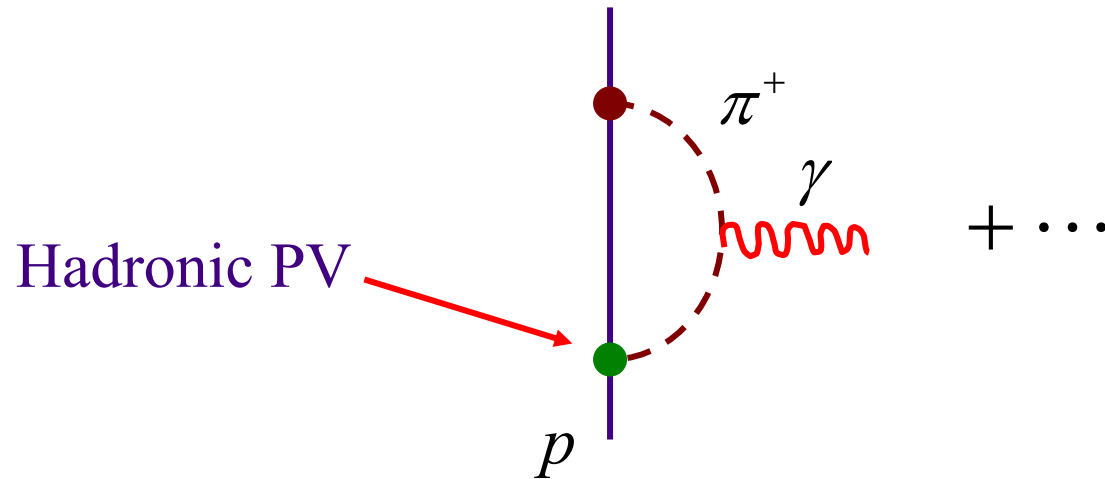
Radiative corrections

R. Hasty et al., Science 290, 2117 (2000).

# Axial Radiative Corrections



# “Anapole” Effects

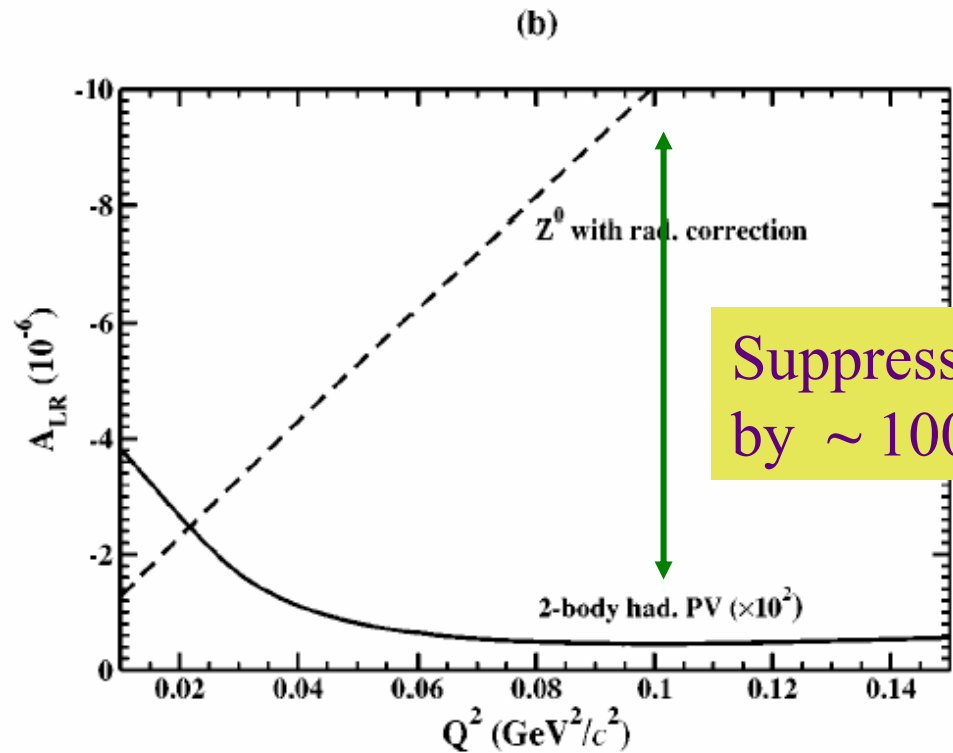
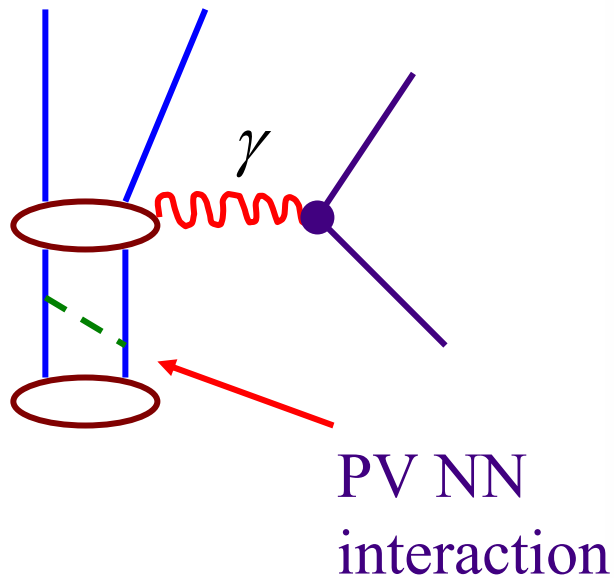


Zhu et al.

Zhu, Puglia, Holstein, R-M ( $\chi$ PT)  
Maekawa & van Kolck ( $\chi$ PT)  
Riska (Model)

Can't account for a large reduction in  $G_A^e$

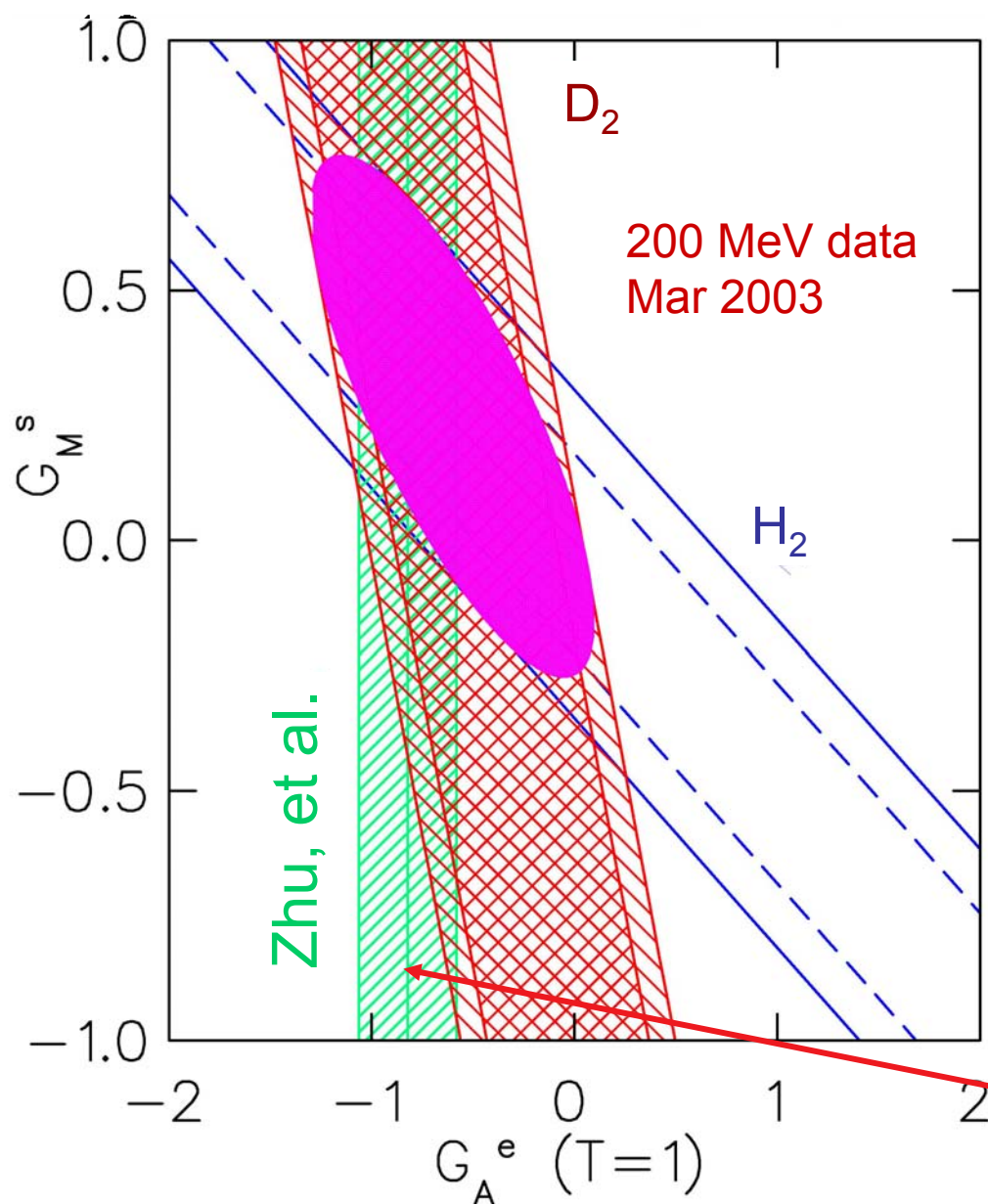
# Nuclear PV Effects



Carlson, Paris, Schiavilla  
Liu, Prezeau, Ramsey-Musolf

## SAMPLE Results

R. Hasty et al., Science 290, 2117 (2000).



at  $Q^2=0.1$  (GeV/c)<sup>2</sup>

- s-quarks contribute less than 5% ( $1\sigma$ ) to the proton's magnetic moment.

**200 MeV update 2003:**  
Improved EM radiative corr.  
Improved acceptance model  
Correction for  $\pi$  background

**125 MeV:**  
no  $\pi$  background  
similar sensitivity  
to  $G_A^e(T=1)$

**Radiative corrections**

E. Beise, U Maryland

# Strange Quark Form Factors

## Theoretical Challenge:

- Strange quarks don't appear in Quark Model picture of the nucleon
- Perturbation theory may not apply

$$\Lambda_{\text{QCD}} / m_s \sim 1 \quad \text{No HQET}$$

$$m_K / \Lambda_\chi \sim 1/2 \quad \chi\text{PT ?}$$

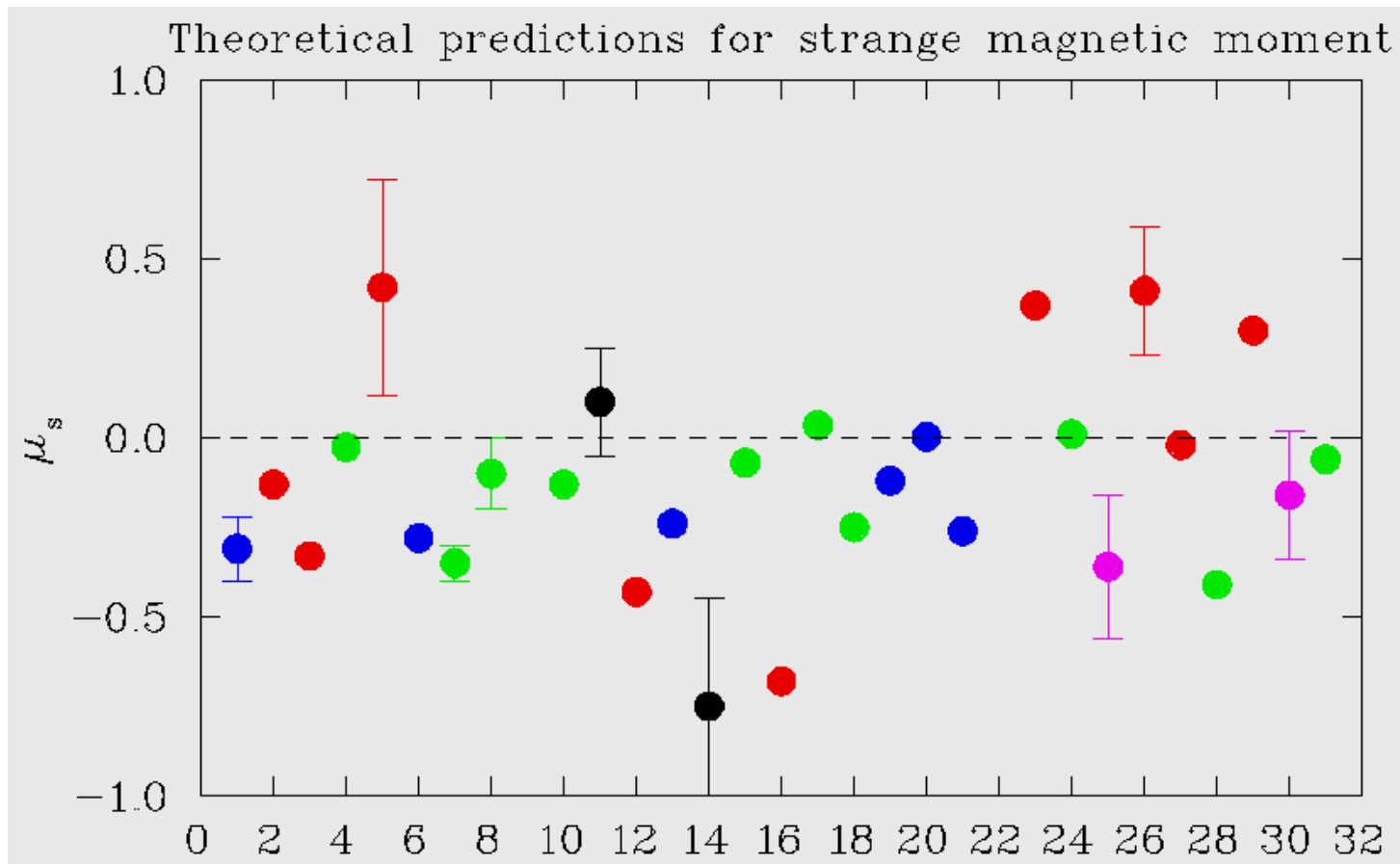
- Symmetry is impotent

$$J_\mu^S = J_\mu^B + 2 J_\mu^{\text{EM}, I=0}$$

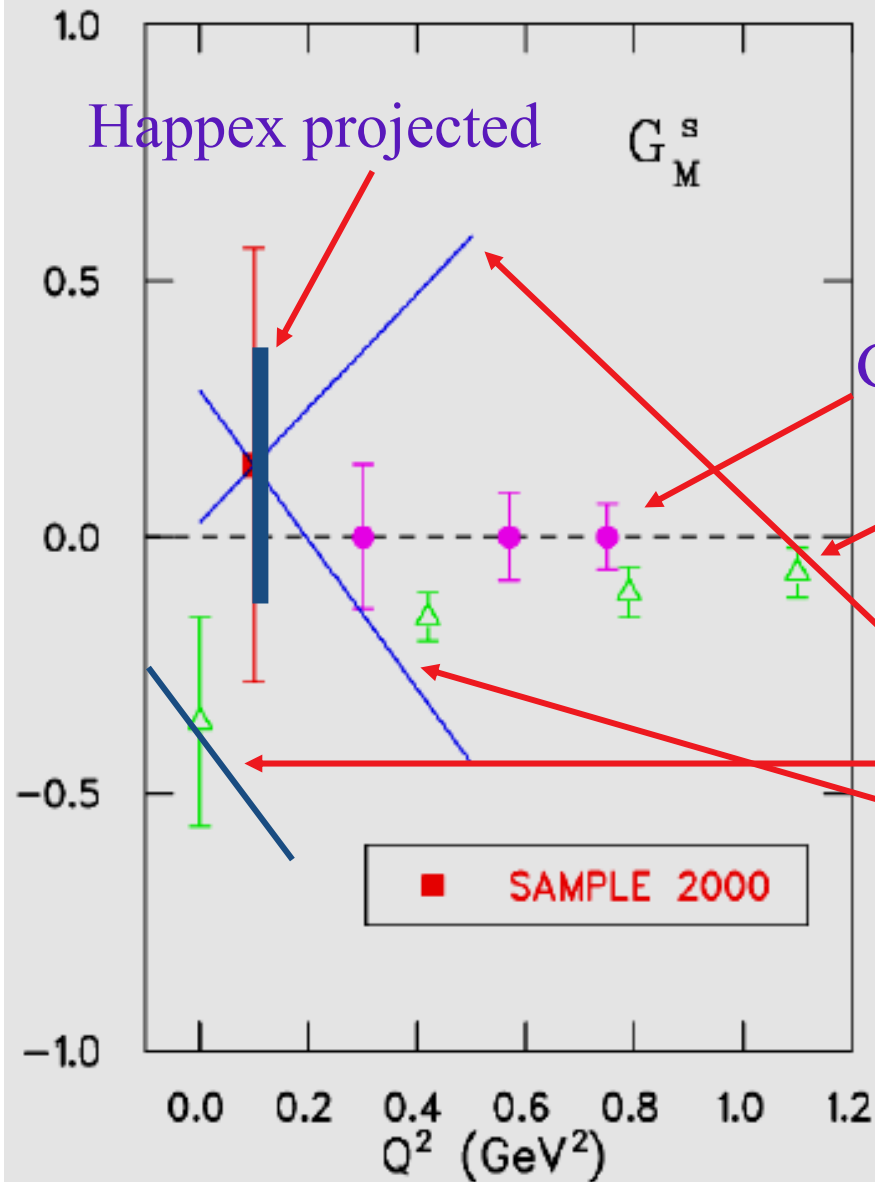


# Theoretical predictions

$$\mu_s \equiv G_M^s(Q^2 = 0)$$



# $Q^2$ -dependence of $G_M^s$



Dispersion theory

Chiral perturbation theory  
"reasonable range" for slope

# What $\chi$ PT can (cannot) say

Strange magnetism as an illustration

Ito, R-M

Hemmert,

Meissner, Kubis

Hammer, Zhu, Puglia, R-M

$$G_M^s(q^s) = \mu_s + \frac{1}{6} q^2 r_{s,M}^2 + \dots$$

$$\mu_s = \left(2M_N/\Lambda_\chi\right) b_s + \dots$$

Unknown low-  
energy constant  
(incalculable)

Kaon loop contributions  
(calculable)

# What $\chi$ PT can (cannot) say

Strange magnetism as an illustration

$$G_M^s(q^s) = \mu_s + \frac{1}{6}q^2 r_{s,M}^2 + \dots$$


$$r_{s,M}^2 = -\frac{6}{\Lambda_\chi} \left\{ \left( \frac{2M_N}{\Lambda_\chi} \right) b_s^r + \frac{1}{18} (5D^2 - 6DF + 9F^2) \left( \frac{\pi M_N}{m_K} + 7 \ln \frac{m_K}{\mu} \right) + \dots \right\}$$

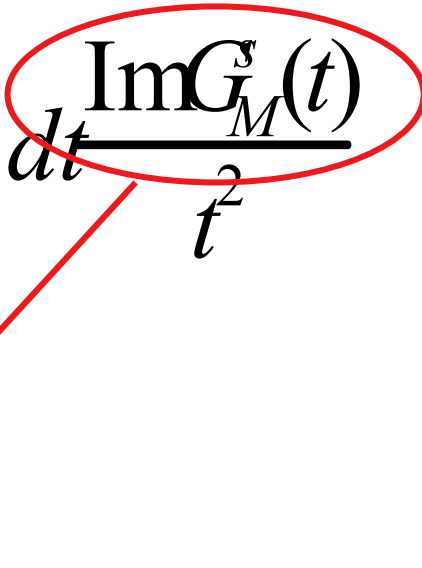
NLO, unknown LEC

LO, parameter free

NLO, cancellation

# Dispersion theory gives a model-independent prediction

Slope of  $G_M^s$  

$$r_{s,M}^2 = \frac{6}{\pi} \int_{9m_\pi^2}^{\infty} dt \frac{\text{Im} G_M^s(t)}{t^2}$$


Strong interaction scattering amplitudes

$e^+ e^- \longrightarrow K^+ K^-$ , etc.

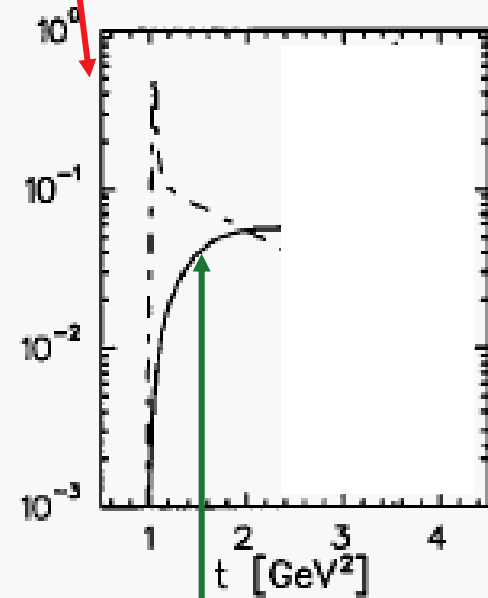
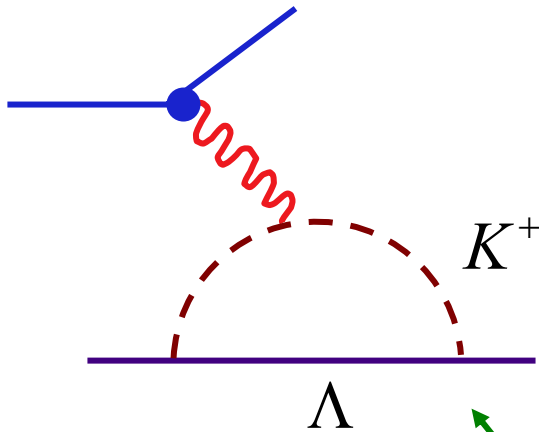
Jaffe

Hammer, Drechsel, R-M

# Dispersion theory gives a model-independent prediction

Hammer & R-M

$$r_{s,M}^2 = \frac{6}{\pi} \int_{4m_K^2}^{\infty} dt \frac{\text{Im} G_M^s(t)}{t^2}$$

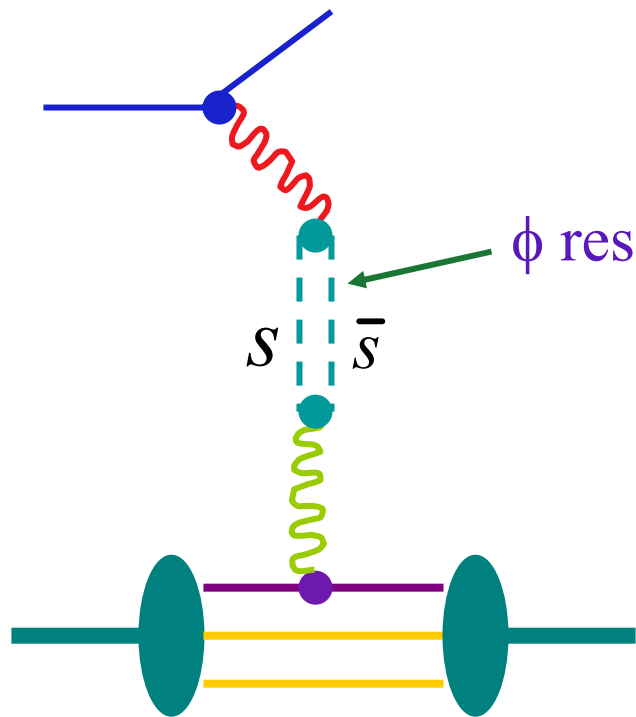


Perturbation theory (1-loop)

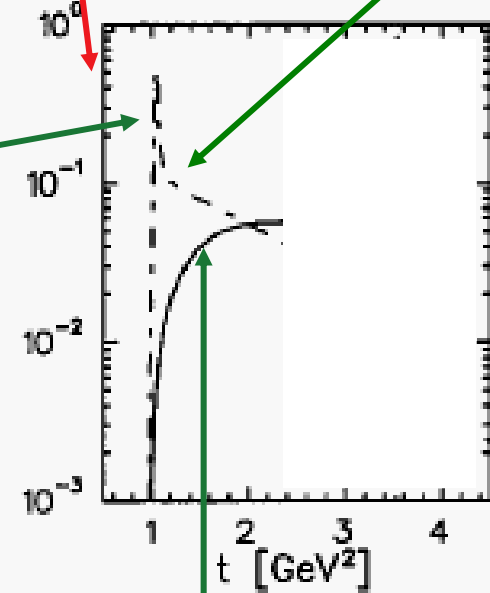
# Dispersion theory gives a model-independent prediction

Hammer & R-M

$$r_{s,M}^2 = \frac{6}{\pi} \int_{4m_K^2}^{\infty} dt \frac{\text{Im} G_M^s(t)}{t^2}$$



$\phi$  resonance



Perturbation theory (1-loop)

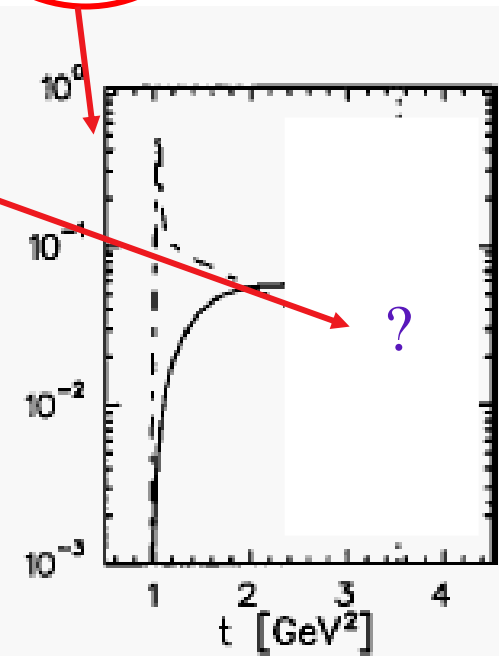
# Dispersion theory gives a model-independent prediction

$$r_{s,M}^2 = \frac{6}{\pi} \int_{4m_K^2}^{\infty} dt \frac{\text{Im} G_M^s(t)}{t^2}$$

Can't do the whole integral

- Are there higher mass excitations of  $s\bar{s}$  pairs?
- Do they enhance or cancel low-lying excitations?

Experiment will give an answer





# PVES and Nucleonic Matter

What is the equation of state of dense nucleonic matter?

We know a lot about the protons, but lack critical information about the neutrons

# PVES and Nucleonic Matter

The  $Z^0$  boson probes neutron properties

Donnelly,  
Dubach, Sick

$$Q_W = Z(1 - 4 \sin^2 \theta_W) + N$$

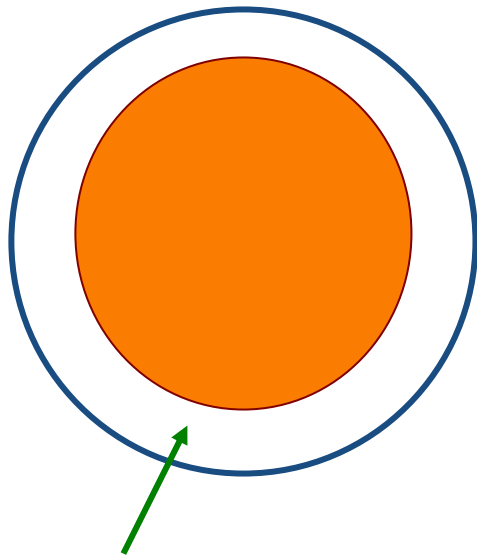
$\sim 0.1$

PREX (Hall A):  $^{208}\text{Pb}$

Horowitz, Pollock,  
Souder, & Michels

# PVES and Neutron Stars

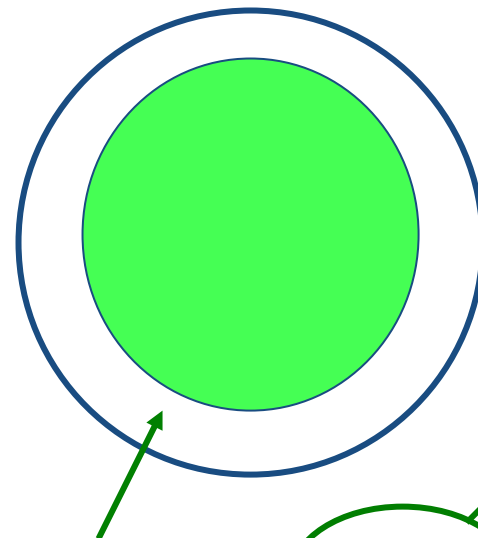
Neutron star



Crust thickness  
decreases with  $P_n$

Horowitz &  
Piekarewicz

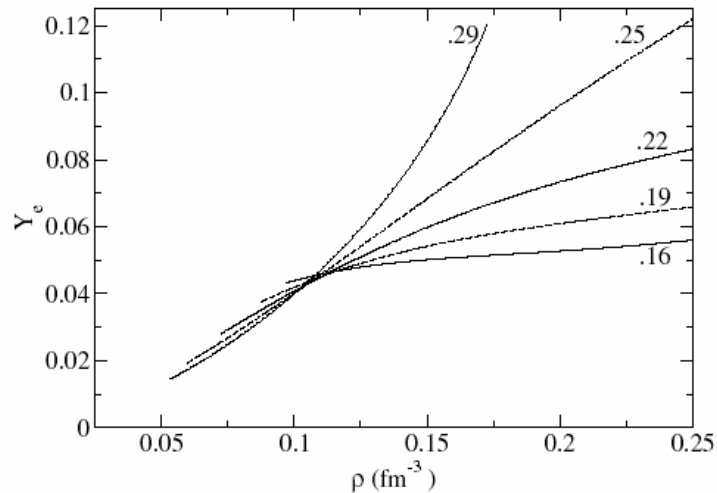
$^{208}\text{Pb}$



Skin thickness  $(R_n - R_p)$   
increases with  $P_n$

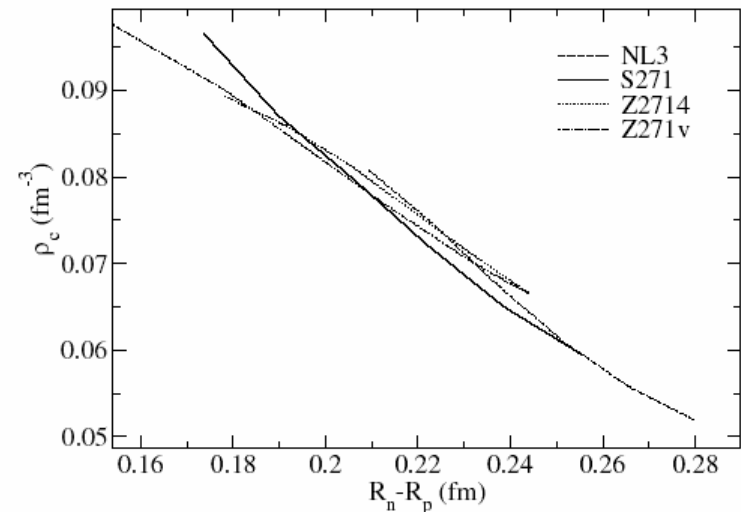
PREX

# PVES and Neutron Stars



Neutron star properties  
are connected to density-  
dependence of symmetry  
energy

Horowitz &  
Piekarewicz



PREX probes  $R_n - R_p$   
a meter of  $E(\rho)$

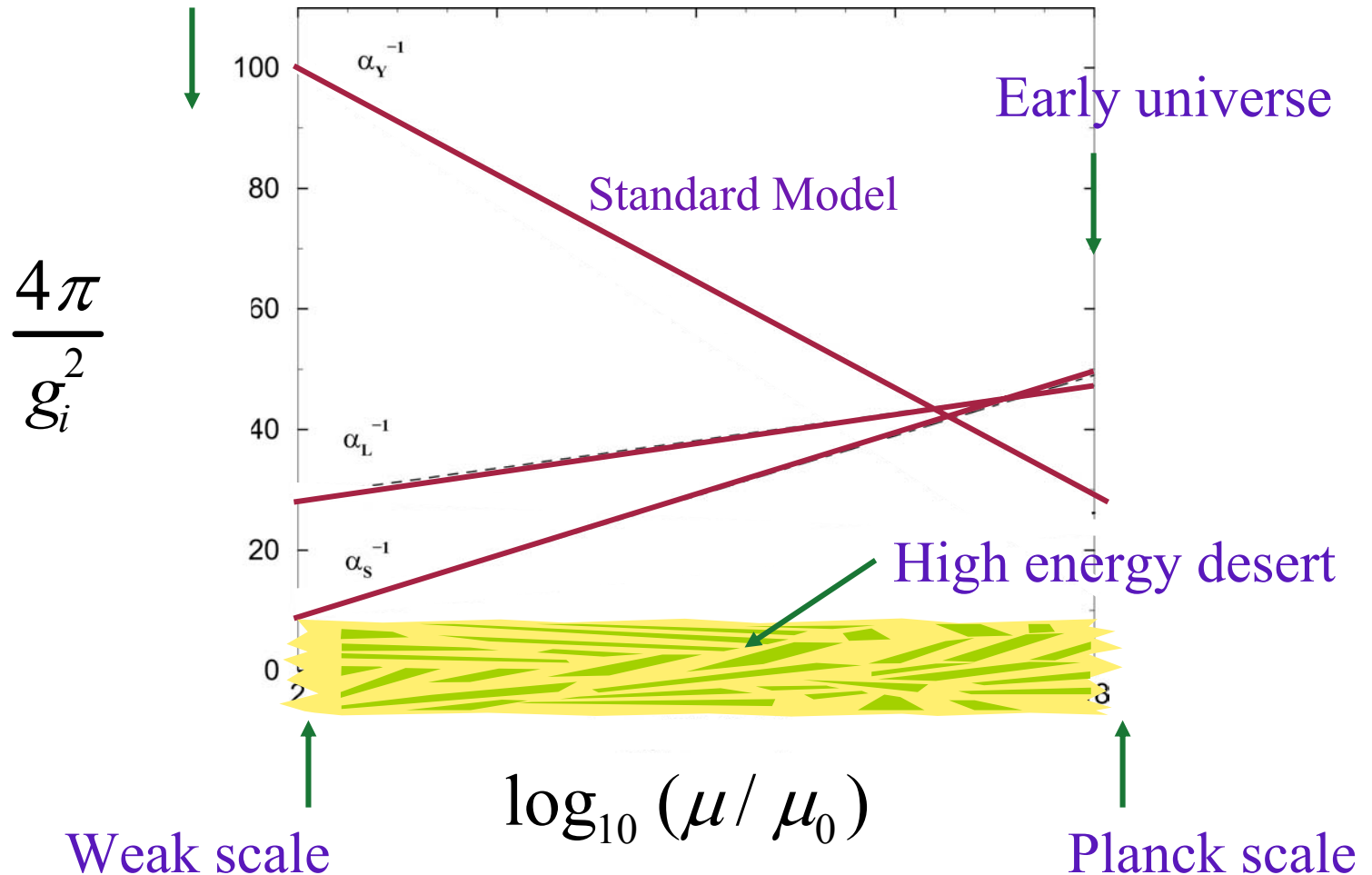
# PVES and the New Standard Model

We believe in the Standard Model, but it leaves many unanswered questions

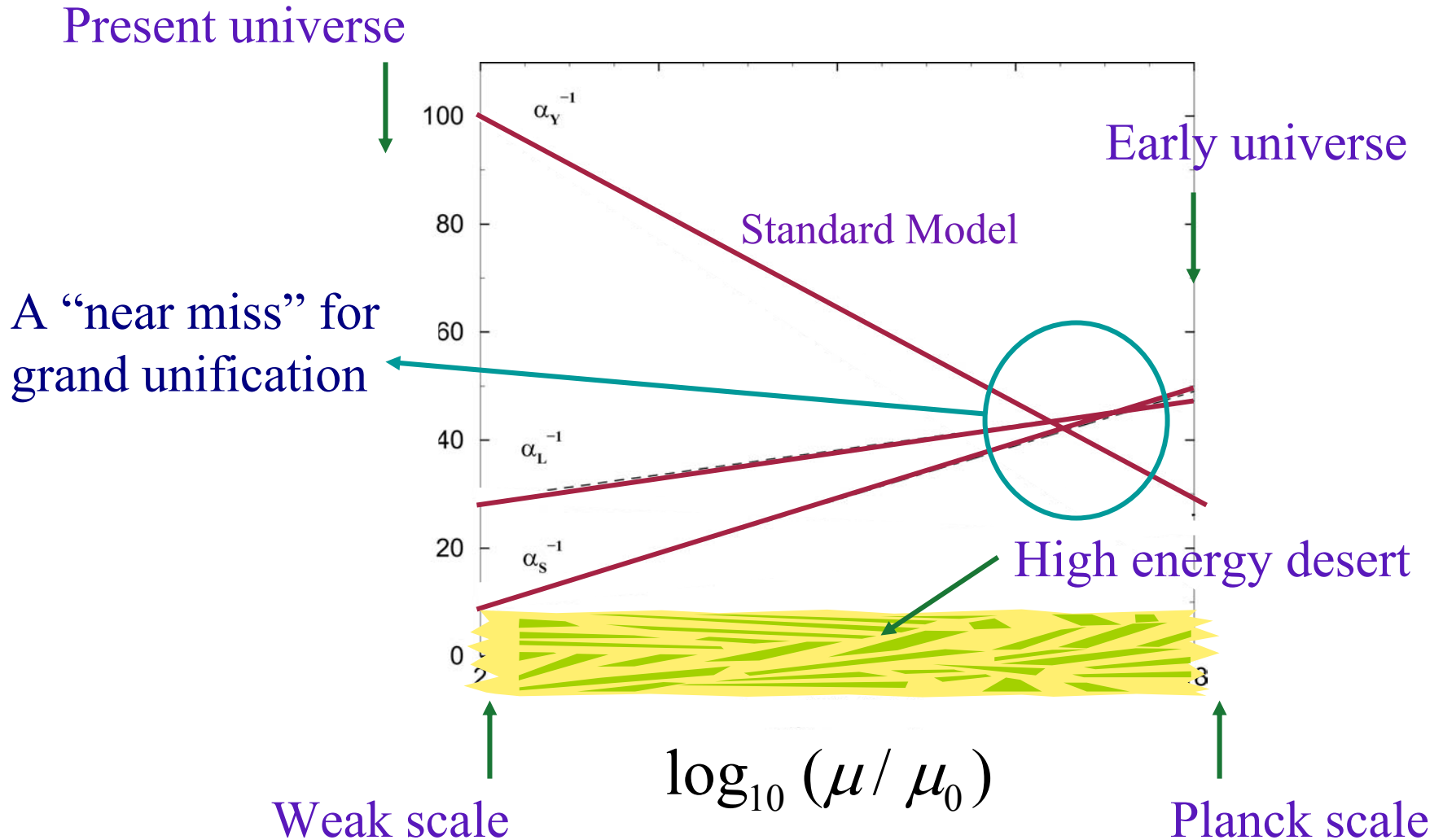
- What were the symmetries of the early Universe and how were they broken?
- What is dark matter?
- Why is there more matter than anti-matter?

# PVES and the New Standard Model

Present universe



# PVES and the New Standard Model



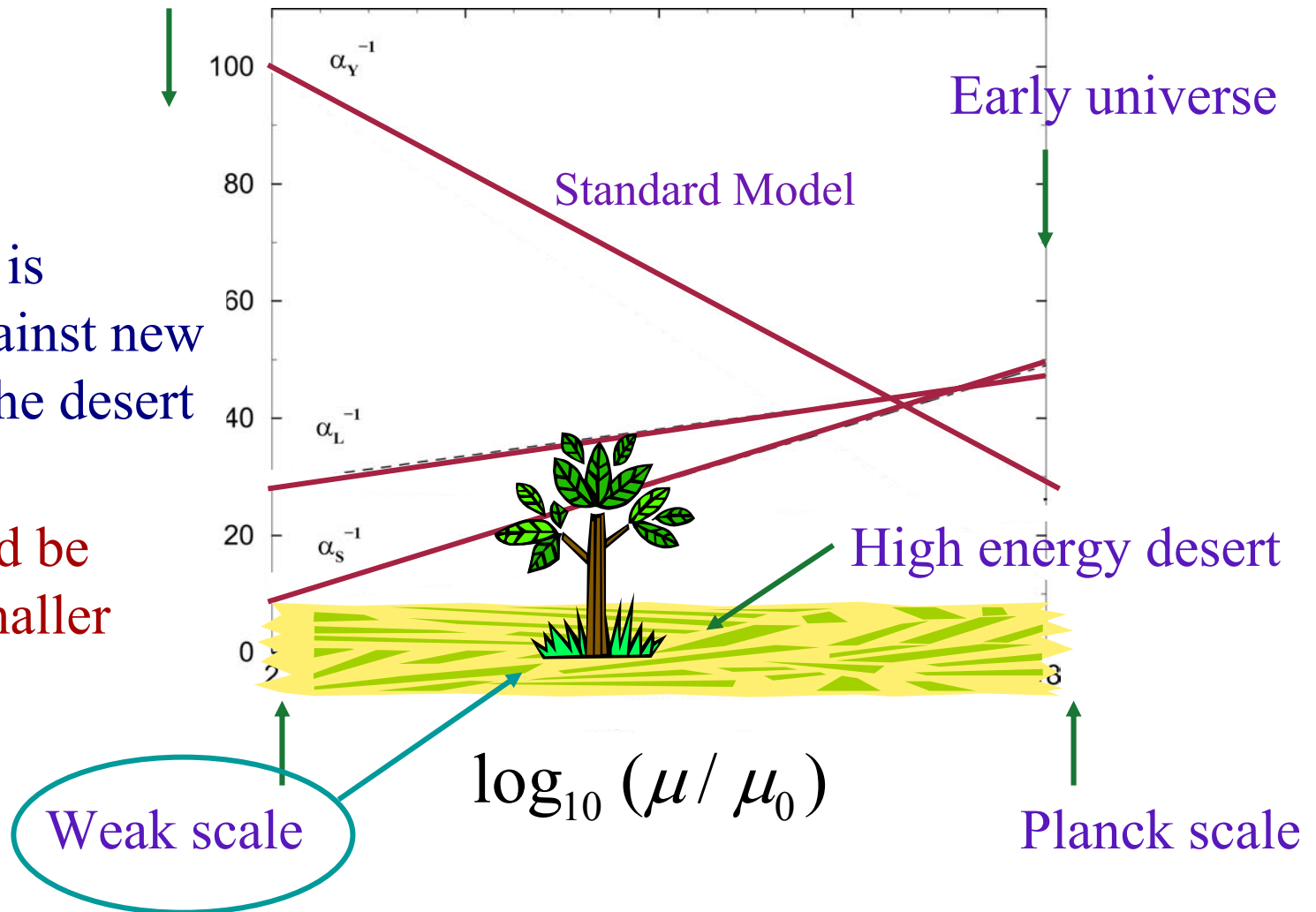
# PVES and the New Standard Model

Present universe

Early universe

Weak scale is  
unstable against new  
physics in the desert

$G_F$  would be  
much smaller





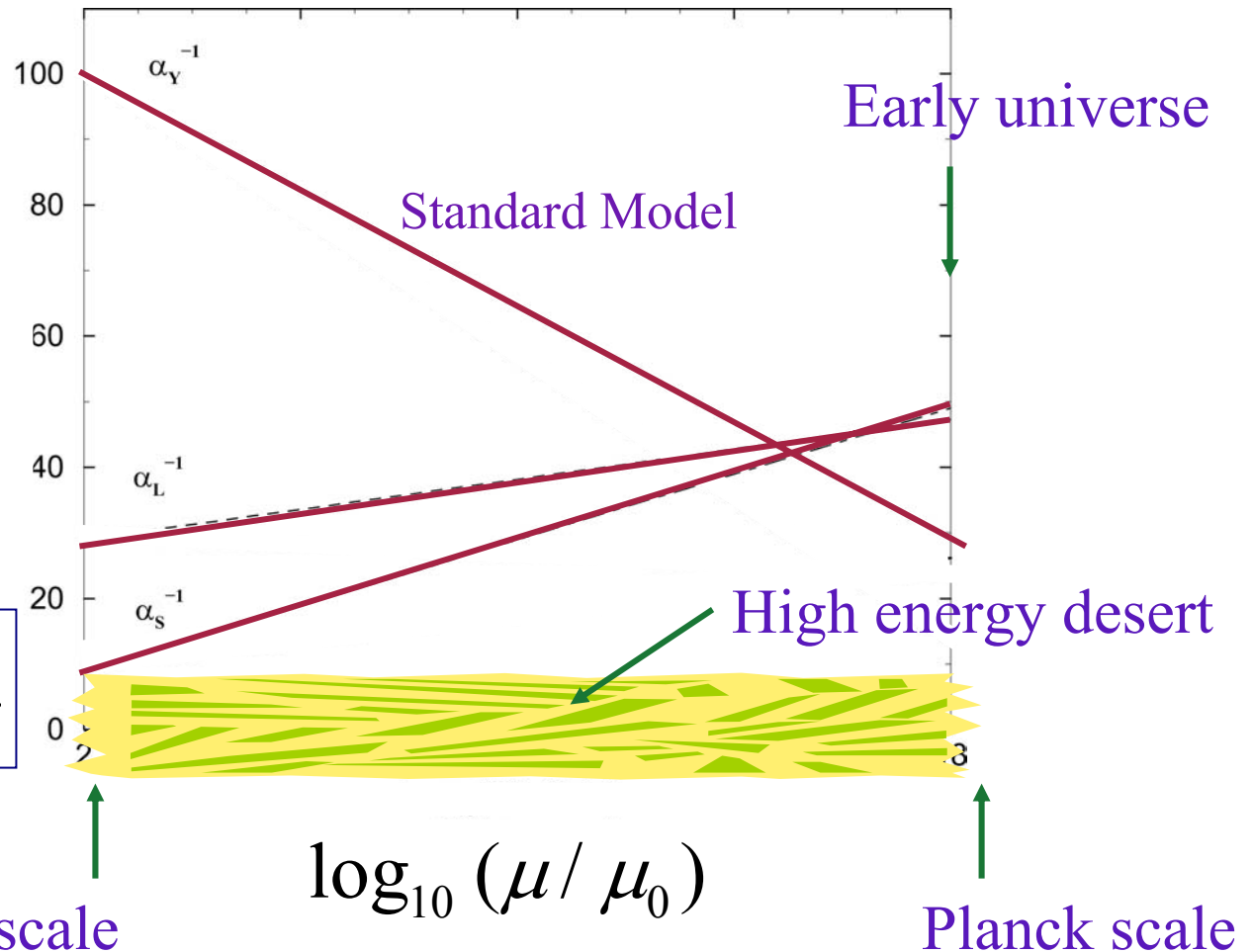
# PVES and the New Standard Model

Present universe

Not enough  
CP-violation  
for weak scale  
baryogenesis

$$n_B - n_{\bar{B}} \sim 10^{10} n_\gamma$$

Weak scale



# Neutral current mixing depends on electroweak symmetry

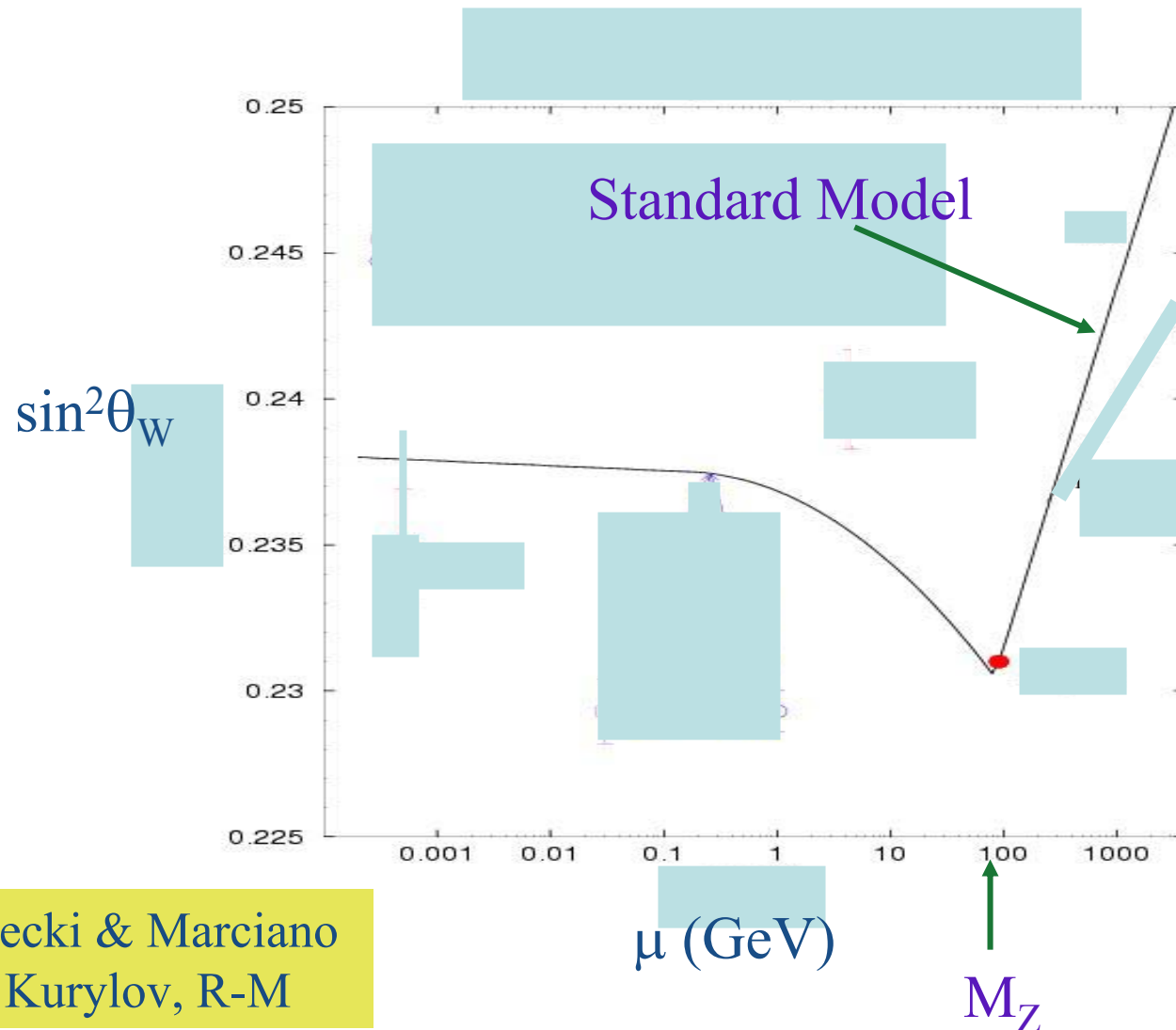
$$J_\mu^{\text{WNC}} = J_\mu^0 + 4 Q \sin^2 \theta_W J_\mu^{\text{EM}}$$

$$\sin^2 \theta_W = \frac{g_Y^2}{g^2 + g_Y^2}$$

$SU(2)_L$

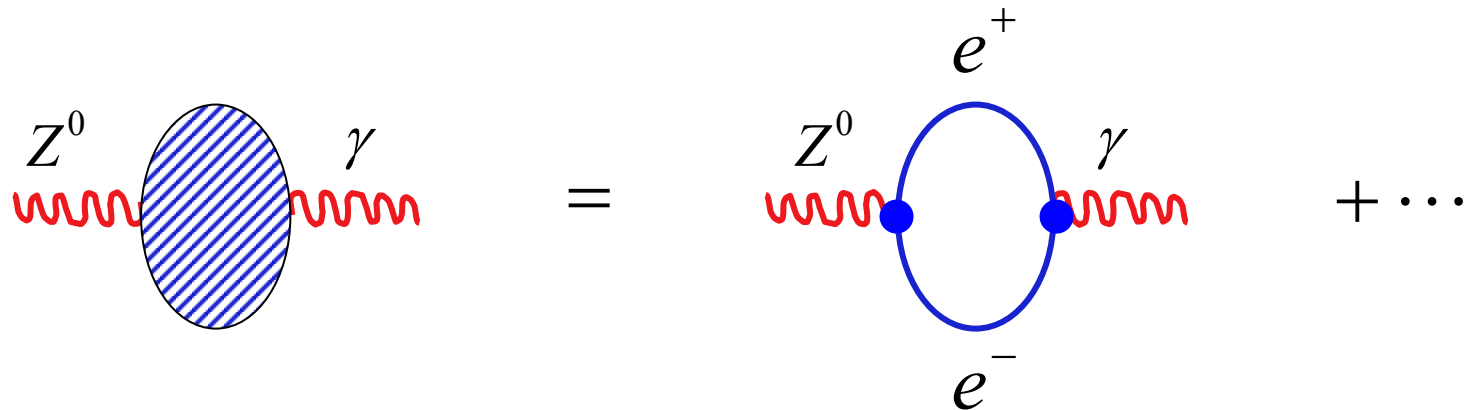
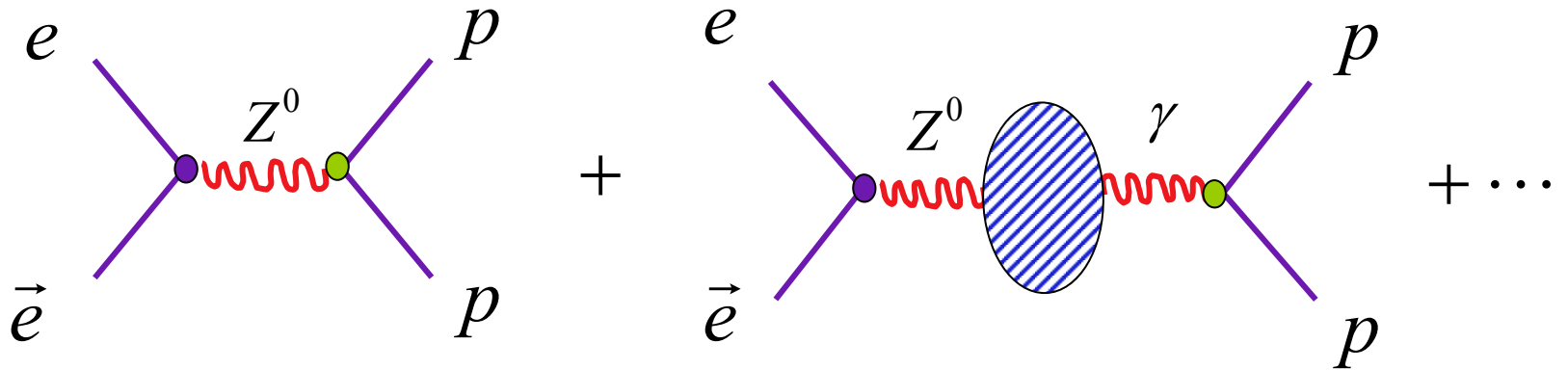
$U(1)_Y$

# Weak mixing also depends on scale

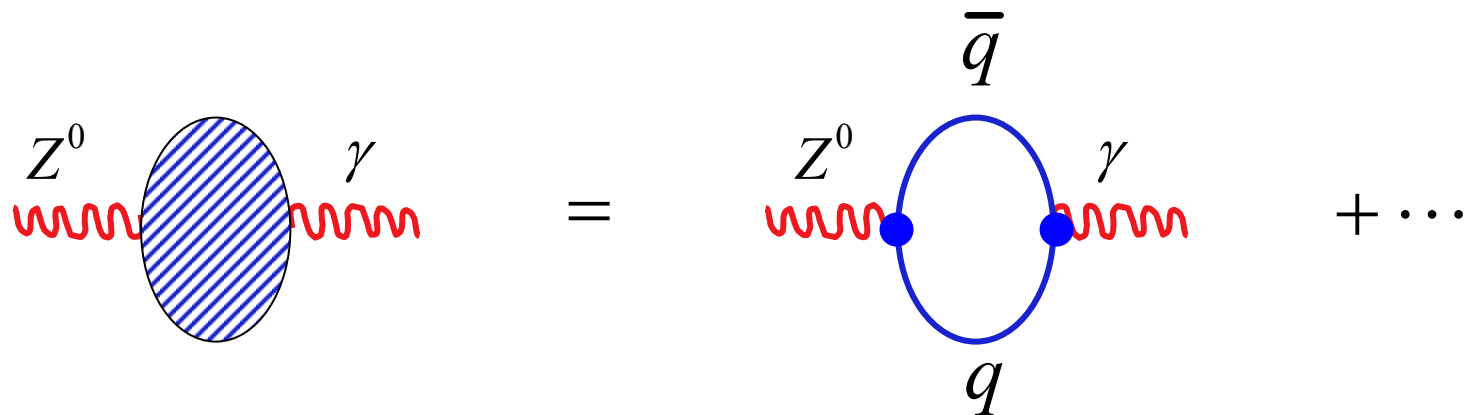
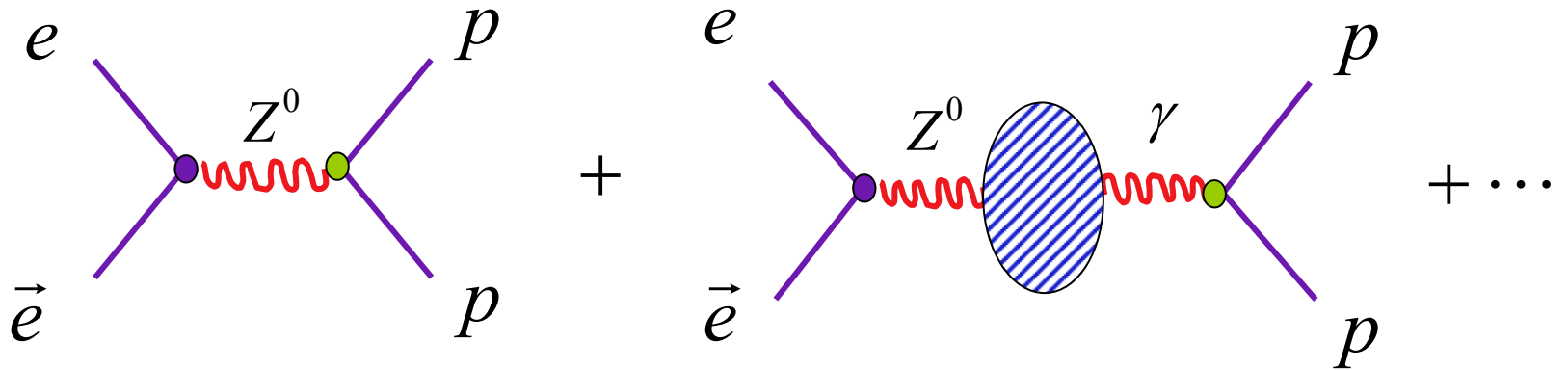


Czarnecki & Marciano  
Erler, Kurylov, R-M

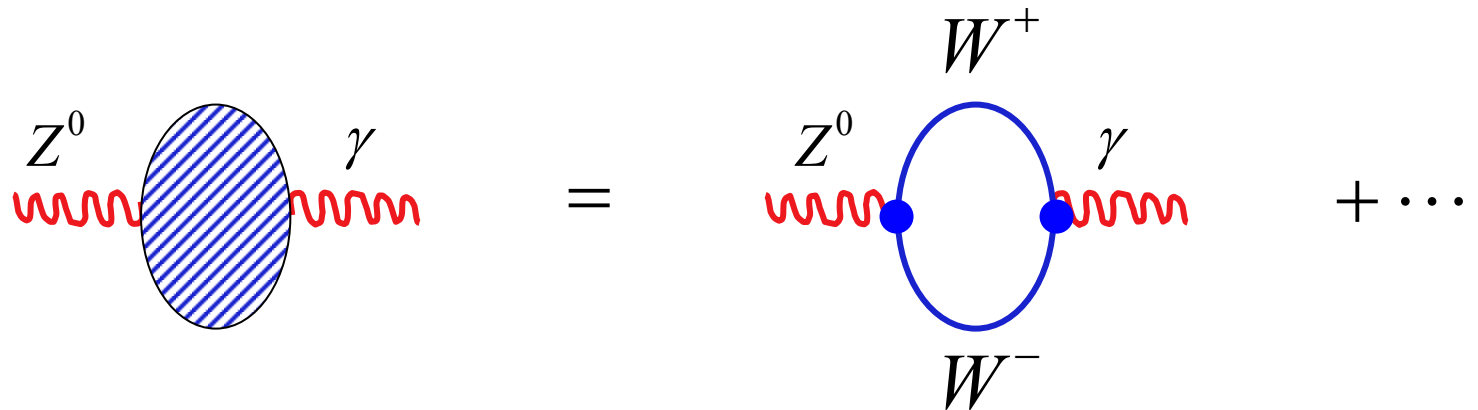
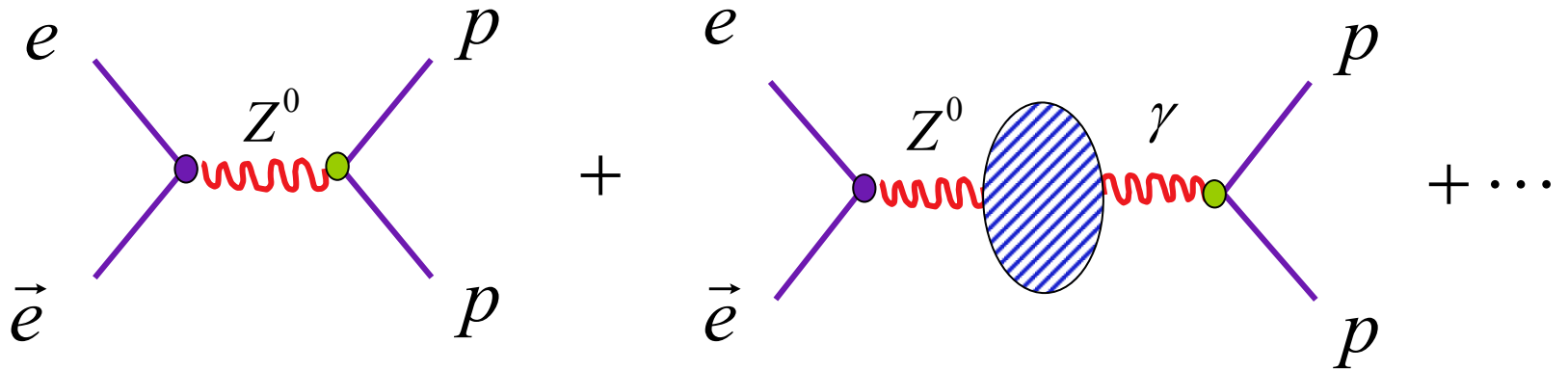
# $\sin^2\theta_w(\mu)$ depends on particle spectrum



# $\sin^2\theta_w(\mu)$ depends on particle spectrum



# $\sin^2\theta_w(\mu)$ depends on particle spectrum



# New Physics & Parity Violation

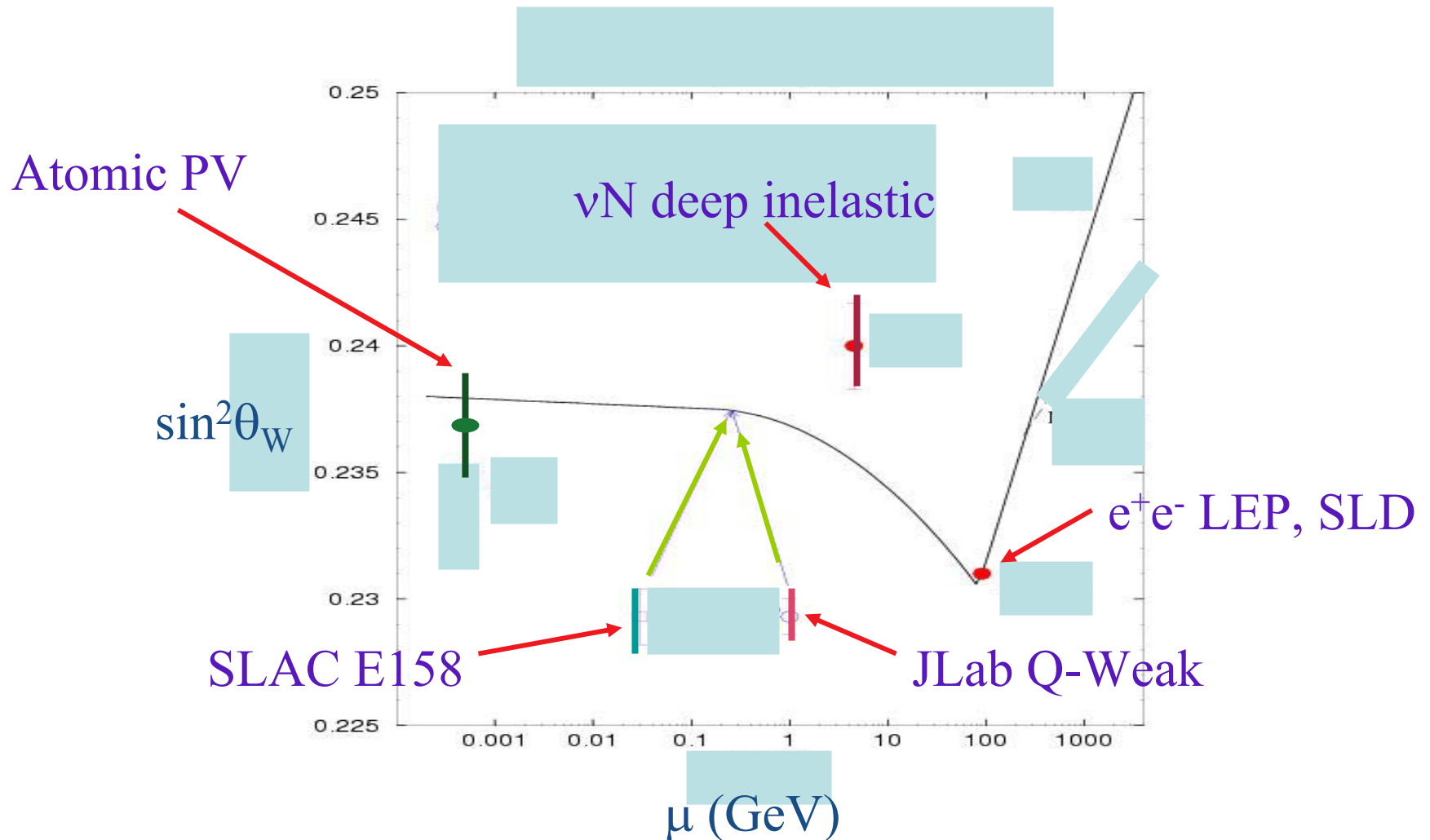
$$Q_W^e = -1 + 4 \sin^2 \theta_W$$

$$Q_W^p = 1 - 4 \sin^2 \theta_W$$

$$Q_W^{Cs} = Z(1 - 4 \sin^2 \theta_W) - N$$

$\sin^2 \theta_W$  is scale-dependent

# Weak mixing also depends on scale





# Additional symmetries in the early universe can change scale-dependence

## Supersymmetry

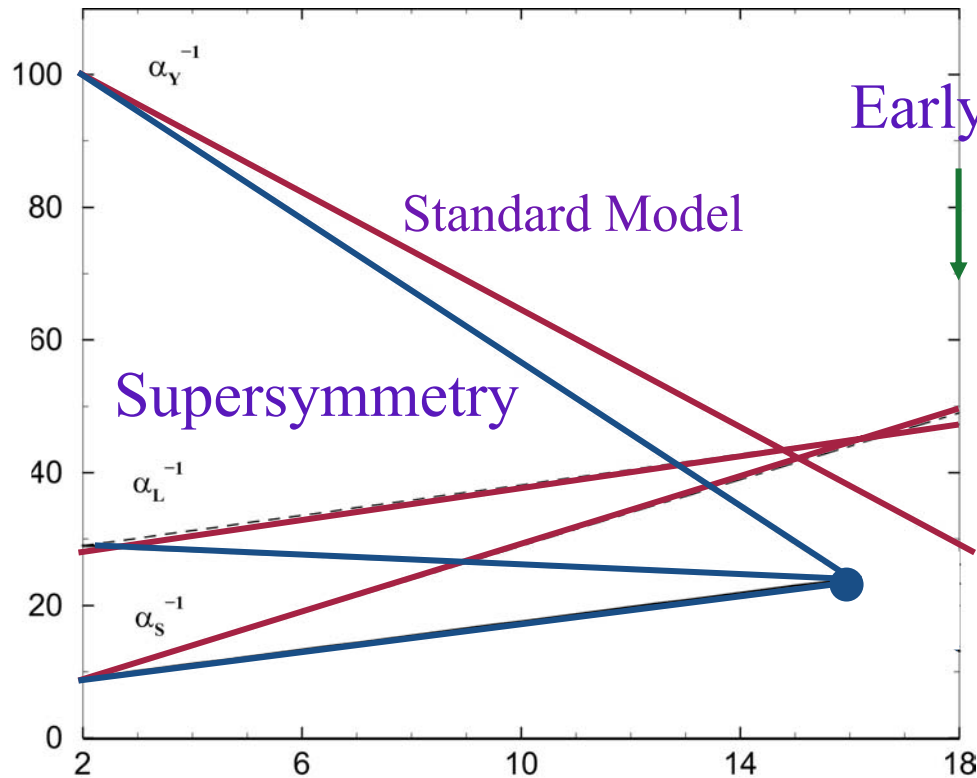
	<u>Fermions</u>		<u>Bosons</u>	
	$e_{L,R}, q_{L,R}$	$\longleftrightarrow$	$\tilde{e}_{L,R}, \tilde{q}_{L,R}$	sfermions
gauginos	$\tilde{W}, \tilde{Z}, \tilde{\gamma}, \tilde{g}$	$\longleftrightarrow$	$W, Z, \gamma, g$	
Higgsinos	$\tilde{H}_u, \tilde{H}_d$	$\longleftrightarrow$	$H$	
$\tilde{W}, \tilde{Z}, \tilde{\gamma}, \tilde{H}_{u,d} \Rightarrow \tilde{\chi}^{\pm}, \tilde{\chi}^0$				Charginos, neutralinos

# Electroweak & strong couplings unify with supersymmetry

Present universe

$$\frac{4\pi}{g_i^2}$$

Weak scale &  
 $G_F$  are protected



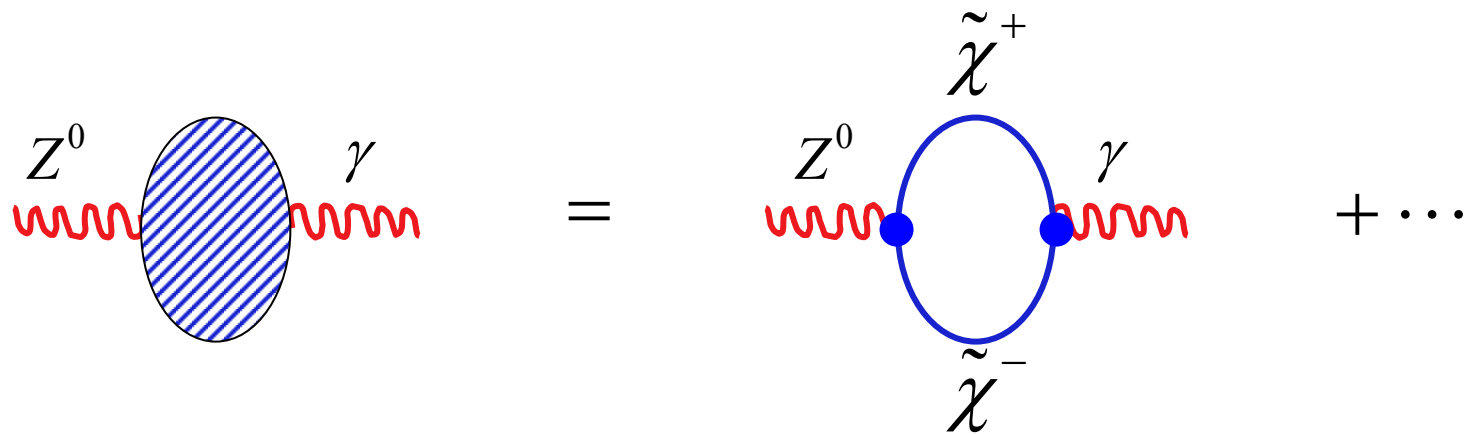
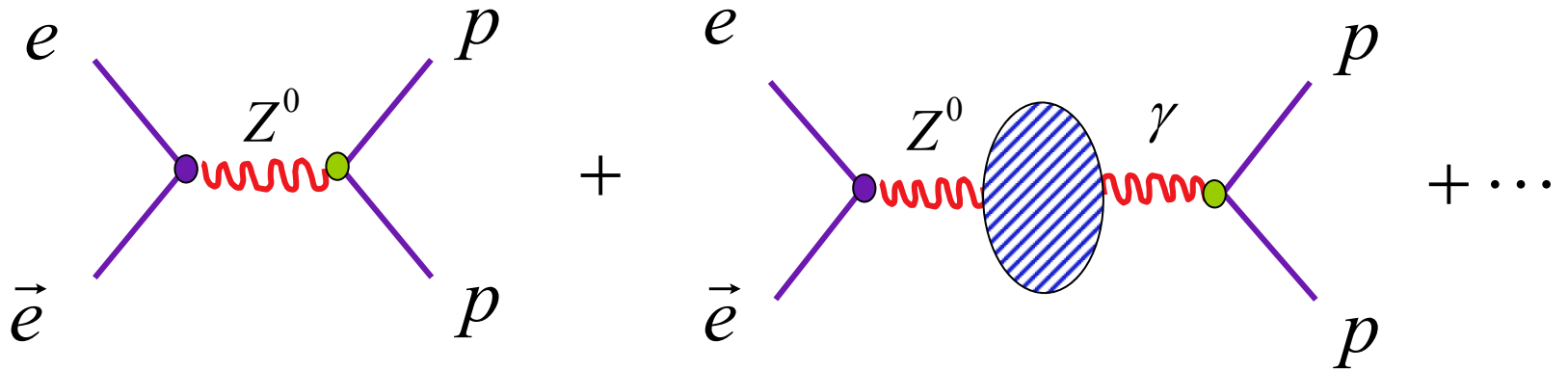
Early universe

$$\log_{10}(\mu/\mu_0)$$

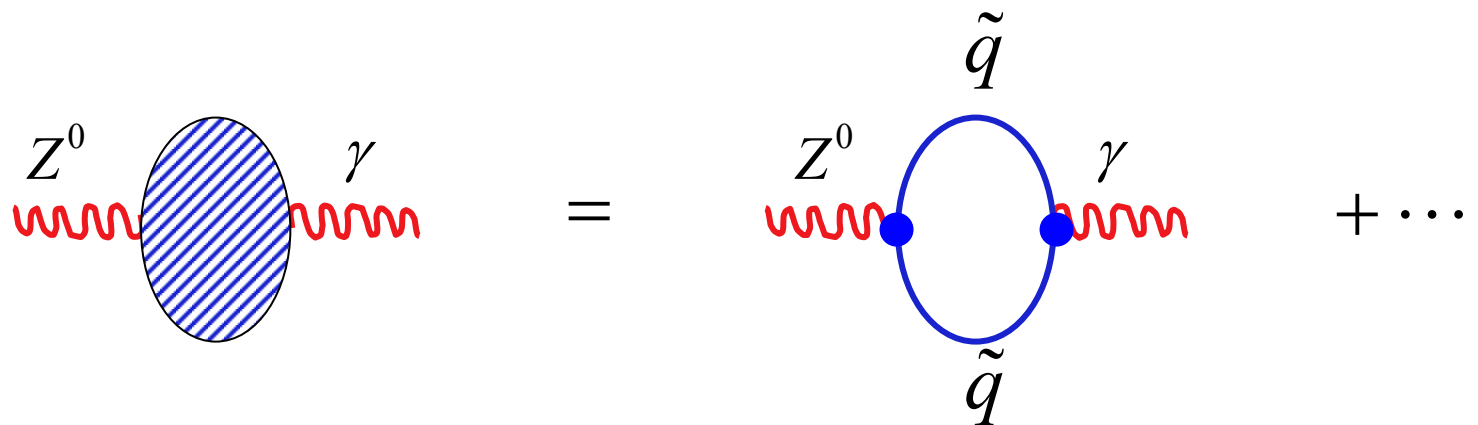
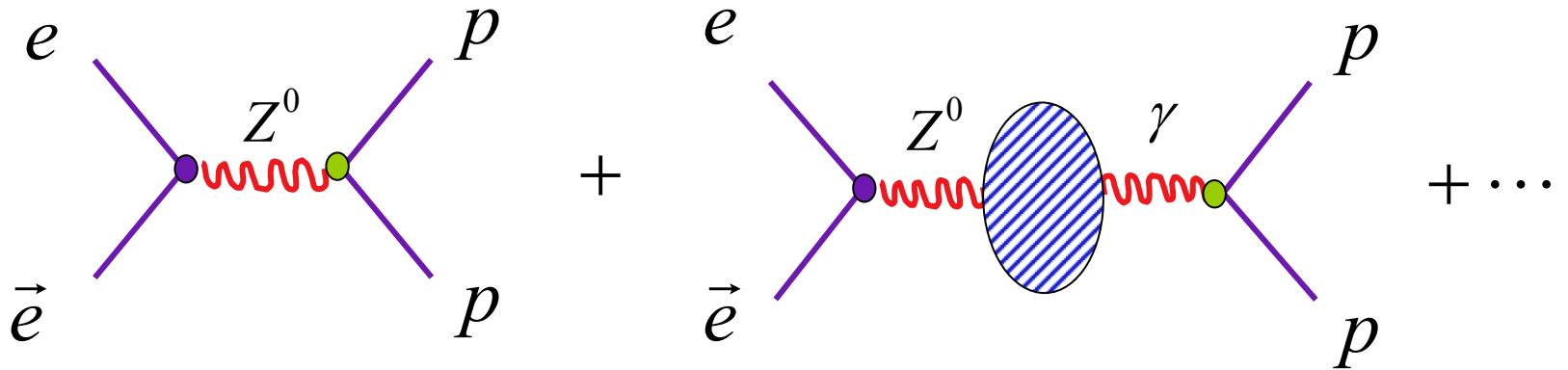
Weak scale

Planck scale

# SUSY will change $\sin^2\theta_w(\mu)$ evolution



# SUSY will change $\sin^2\theta_w(\mu)$ evolution



# Comparing $Q_w^e$ and $Q_w^p$

Kurylov, R-M, Su

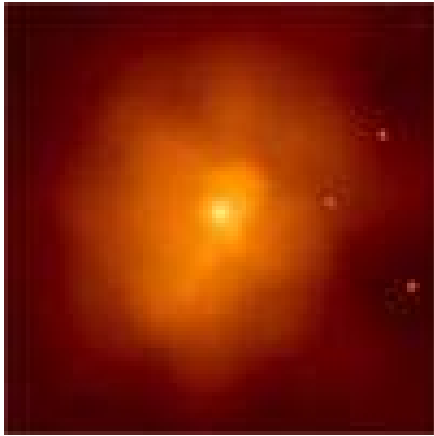
SUSY loops



QuickTime™ and a TIFF (Uncompressed) decompressor are needed to see this picture.

3000 randomly chosen  
SUSY parameters but  
effects are correlated

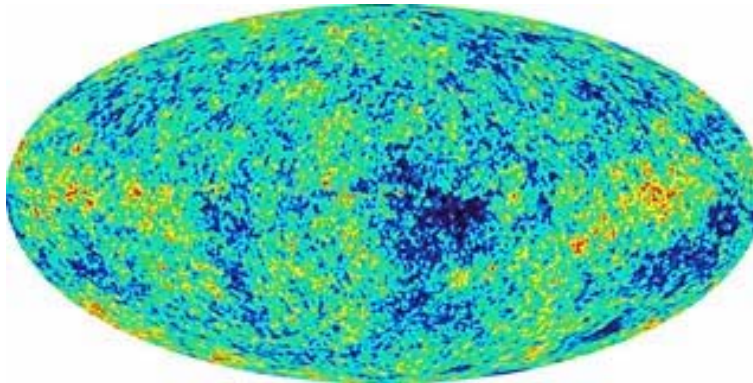
# Can SUSY explain dark matter?



Expansion



Rotation curves



Cosmic microwave  
background

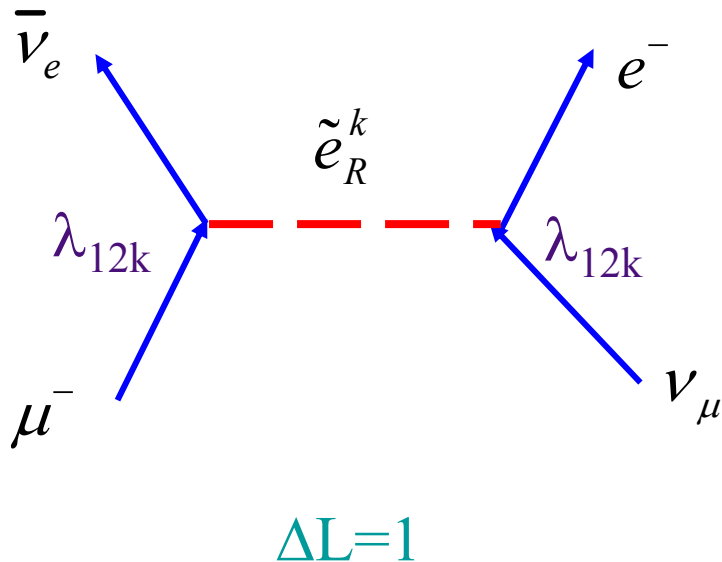
# SUSY provides a DM candidate

$\tilde{\chi}^0$       Neutralino

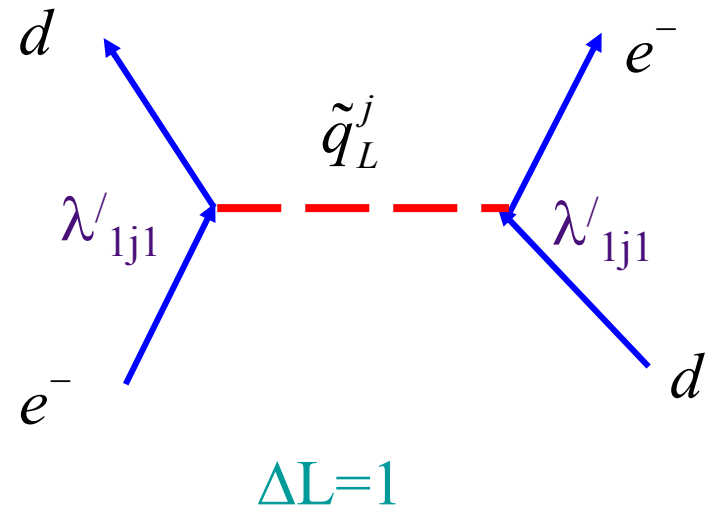
- Stable, lightest SUSY particle if baryon (B) and lepton (L) numbers are conserved
- However, B and L need not be conserved in SUSY, leading to neutralino decay

e.g.  $\tilde{\chi}^0 \rightarrow e^+ \mu^- \nu_e$

# B and/or L Violation in SUSY can also affect low-energy weak interactions



$\mu$ -decay,  $\beta$ -decay,...



$Q_W^P$  in PV electron scattering



# Comparing $Q_w^e$ and $Q_w^p$

Kurylov, R-M, Su

SUSY loops



No SUSY  
dark matter

$\chi^0 \rightarrow e\mu^+\nu_e$

QuickTime™ and a TIFF (Uncompressed) decompressor are needed to see this picture.

$\nu$  is Majorana



RPV 95% CL

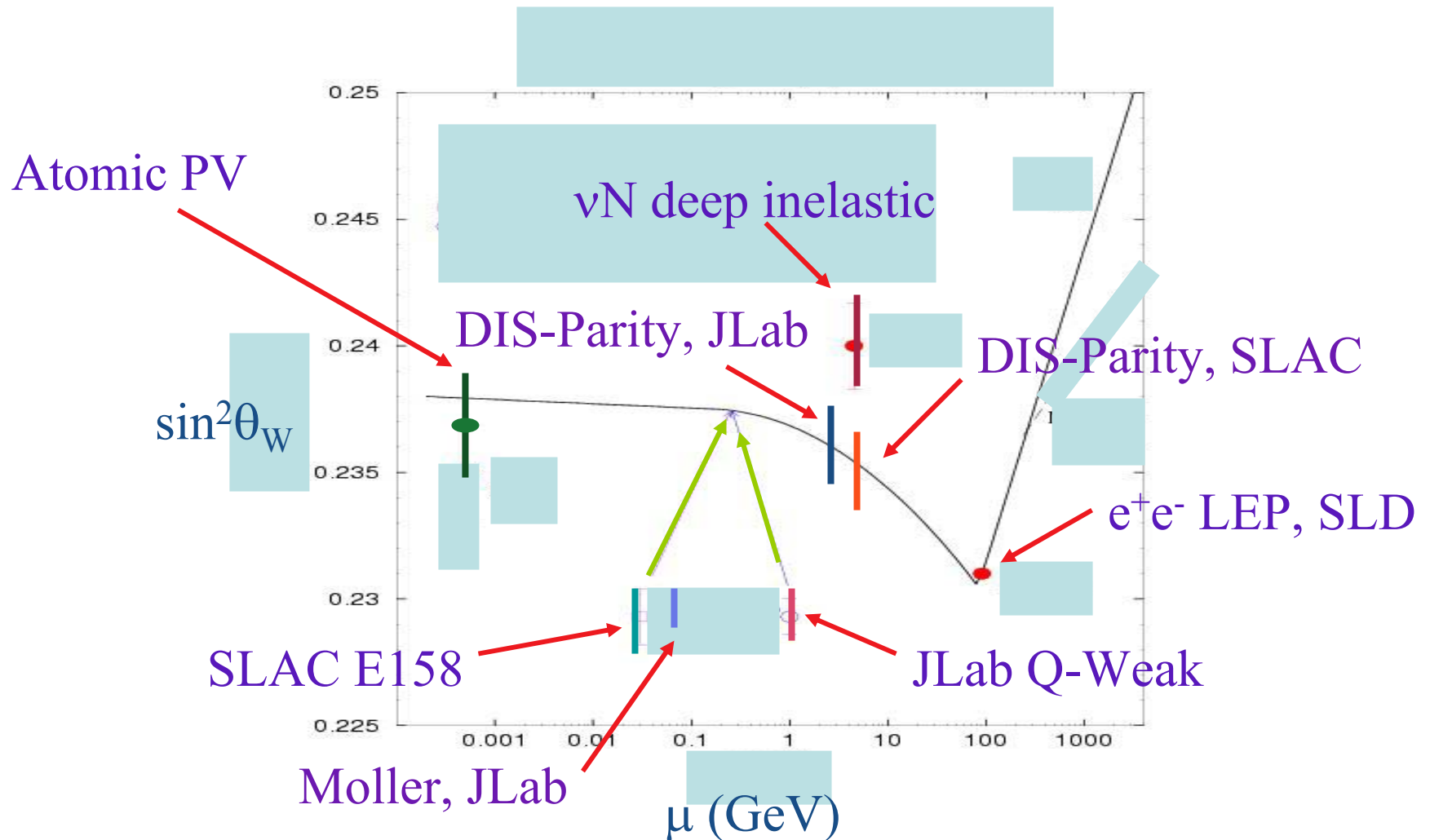
# Comparing $Q_w^e$ and $Q_w^p$

Can be a *diagnostic tool* to determine whether or not

- the early Universe was *supersymmetric*
- there is *supersymmetric* dark matter

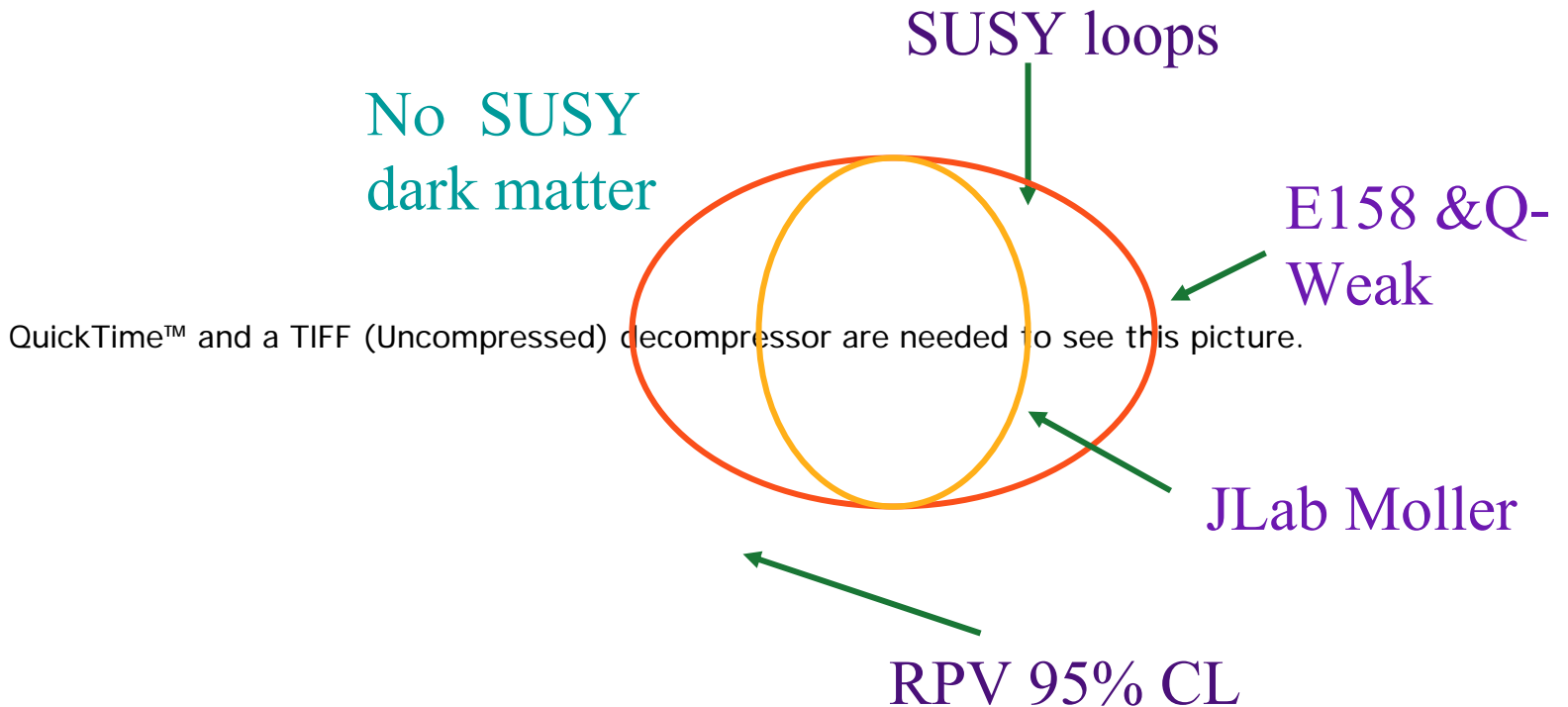
The weak charges can serve a similar diagnostic purpose for other models for high energy symmetries, such as *left-right symmetry, grand unified theories with extra  $U(1)$  groups*, etc.

# Weak mixing also depends on scale



# Comparing $Q_w^e$ and $Q_w^p$

Kurylov, R-M, Su



# Interpretation of precision measurements

How well do we now the SM predictions? Some QCD issues

## Proton Weak Charge

$$A_{LR} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} [Q_W^p + F^p(Q^2, \theta)]$$

Weak charge

Form factors: MIT,  
JLab, Mainz

$Q^2=0.03 \text{ (GeV/c)}^2$

$Q^2>0.1 \text{ (GeV/c)}^2$

# Interpretation of precision measurements

How well do we now the SM predictions? Some QCD issues

Proton Weak Charge

$$A_{LR} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} [Q_W^p + F^p(Q^2, \theta)]$$

$$F^p(Q^2, \theta \rightarrow 0) \sim Q^2$$

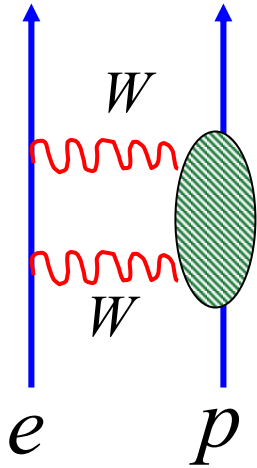
Use  $\chi$ PT to extrapolate in small  $Q^2$  domain and current PV experiments to determine LEC's

# Summary

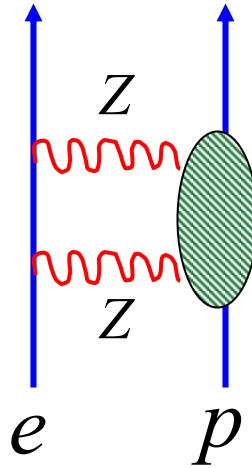
- Parity-violating electron scattering provides us with a well-understood tool for studying several questions at the forefront of nuclear physics, particle physics, and astrophysics:
  - Are sea quarks relevant at low-energies?
  - How compressible is neutron-rich matter
  - What are the symmetries of the early Universe?
- Jefferson Lab is *the* parity violation facility
- We have much to look forward to in the coming years

# QCD Effects in $Q_W^P$

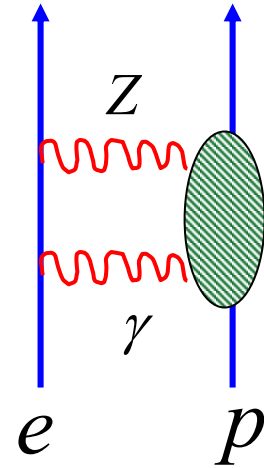
Box graphs



$$\delta Q_W \sim 26\%$$



$$\delta Q_W \sim 3\%$$



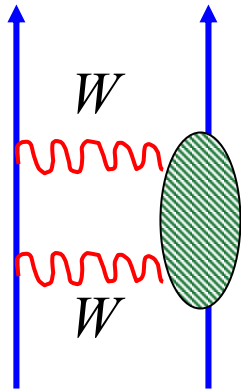
$$\delta Q_W \sim 6\%$$

$k_{\text{loop}} \sim M_W$  : pQCD

$\Lambda_{\text{QCD}} < k_{\text{loop}} < M_W$  :  
non-perturbative



# Box graphs, cont'd.



Protected by symmetry

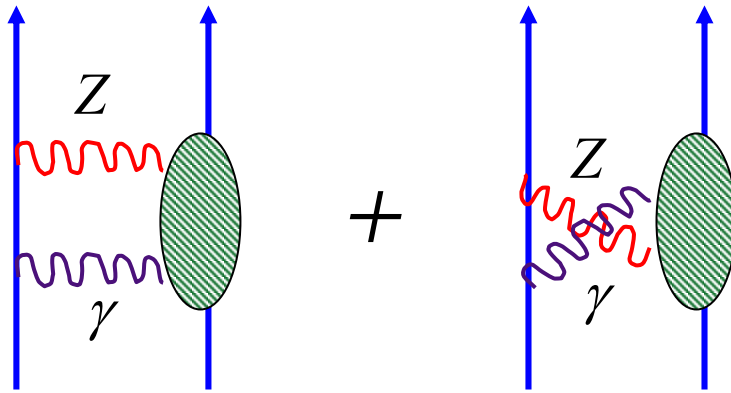
$$M_{WW} = -\frac{G_F}{2\sqrt{2}} \frac{\hat{\alpha}}{4\pi\hat{s}^2} \left[ 2 + 5 \left( 1 - \frac{\alpha_s(M_W^2)}{\pi} \right) \right]$$

Short-distance correction: OPE

$$\delta Q_W^p(\text{QCD}) \sim -0.7\% \quad WW$$

$$\delta Q_W^p(\text{QCD}) \sim -0.08\% \quad ZZ$$

## Box graphs, cont'd.

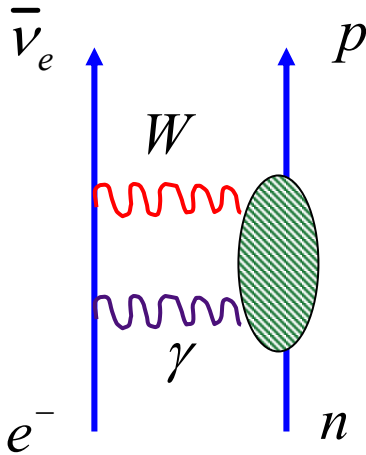


Long-distance physics:  
not calculable

$$M_{Z\gamma} = -\frac{G_F}{2\sqrt{2}} \frac{5\hat{\alpha}}{2\pi} (1 - 4\hat{s}^2) \left[ \ln \left( \frac{M_Z^2}{\Lambda^2} \right) + C_{\gamma Z}(\Lambda) \right]$$

Fortuitous suppression factor: box + crossed  $\sim$   
 $\epsilon^{\mu\nu\alpha\beta} k_\nu J_\alpha^\gamma J_\beta^Z \sim A^\mu \implies g_v^e = (-$   
 $1 + 4 \sin^2 \theta_W)$

# Neutron $\beta$ -decay



$$M_{W\gamma} = \frac{G_F}{\sqrt{2}} \frac{\hat{\alpha}}{2\pi} \left[ \ln \left( \frac{M_Z^2}{\Lambda^2} \right) + C_{\gamma W}(\Lambda) \right]$$

$|\delta C_{\gamma W}| < 2$       to avoid exacerbating CKM  
non-unitarity

$|\delta C_{\gamma Z}| < 2 \Rightarrow \delta Q_W^p < 1.5\%$